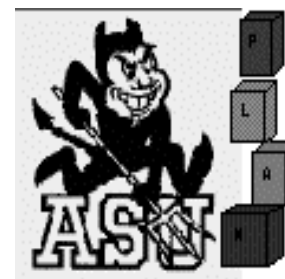


# *Recent Advances in AI Planning: A Unified View*

IJCAI-99 Tutorial



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***<http://rakaposhi.eas.asu.edu/ijcai99-tutorial>***

# Planning is hot...

*26% of the papers in AAAI-99. 20% of papers in IJCAI-99.  
New People. Conferences. Workshops. Competitions.  
Inter-planetary explorations. Why the increased interest?*

## ✧ Significant scale-up in the last 4-5 years

- Before we could synthesize about 5-6 action plans in minutes
- Now, we can synthesize 100-action plans in minutes
  - » Further scale-up with domain-specific control

## ✧ Significant strides in our understanding

- Rich connections between planning and CSP(SAT) OR (ILP)
  - » Vanishing separation between planning & Scheduling
- New ideas for heuristic control of planners
- Wide array of approaches for customizing planners with domain-specific knowledge

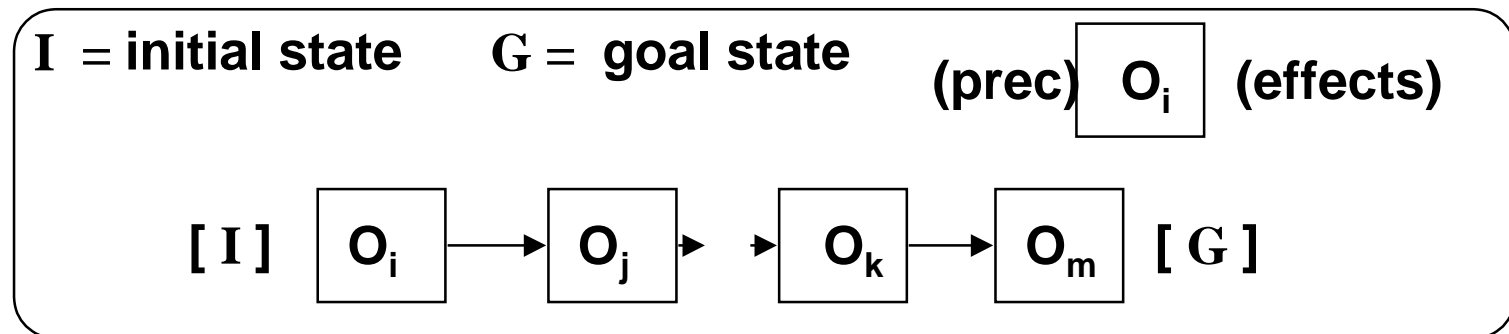
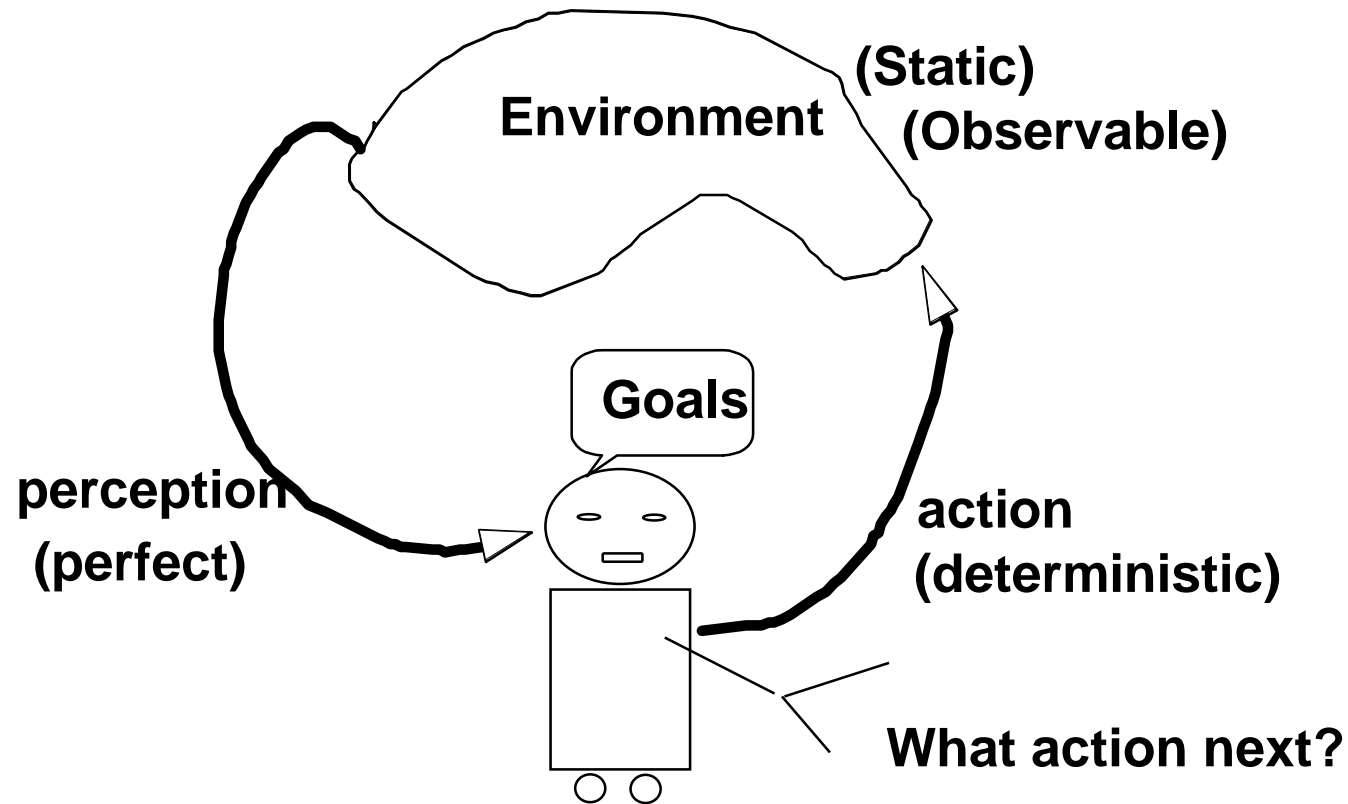
# Overview

- ✧ (Classical) planning problem
  - Modeling, Proving correctness
- ✧ Refinement Planning: Formal Framework
- ✧ Conjunctive refinement planners
  - Heuristics
- ✧ Disjunctive refinement planners
  - Refinement of disjunctive plans
  - Solution extraction from disjunctive plans
    - » Direct, Compiled (SAT, CSP, ILP)
- ✧ Customizing Planners
  - User-assisted Customization
  - Automated customization
- ✧ Support for non-classical worlds

# Planning : The big picture

- ✧ **Synthesizing goal-directed behavior**
- ✧ **Planning involves**
  - Action selection; Handling causal dependencies
  - Action sequencing and handling resource allocation (aka SCHEDULING)
- ✧ **Depending on the problem, plans can be**
  - action sequences
  - or “policies” (action trees, state-action mappings etc.)

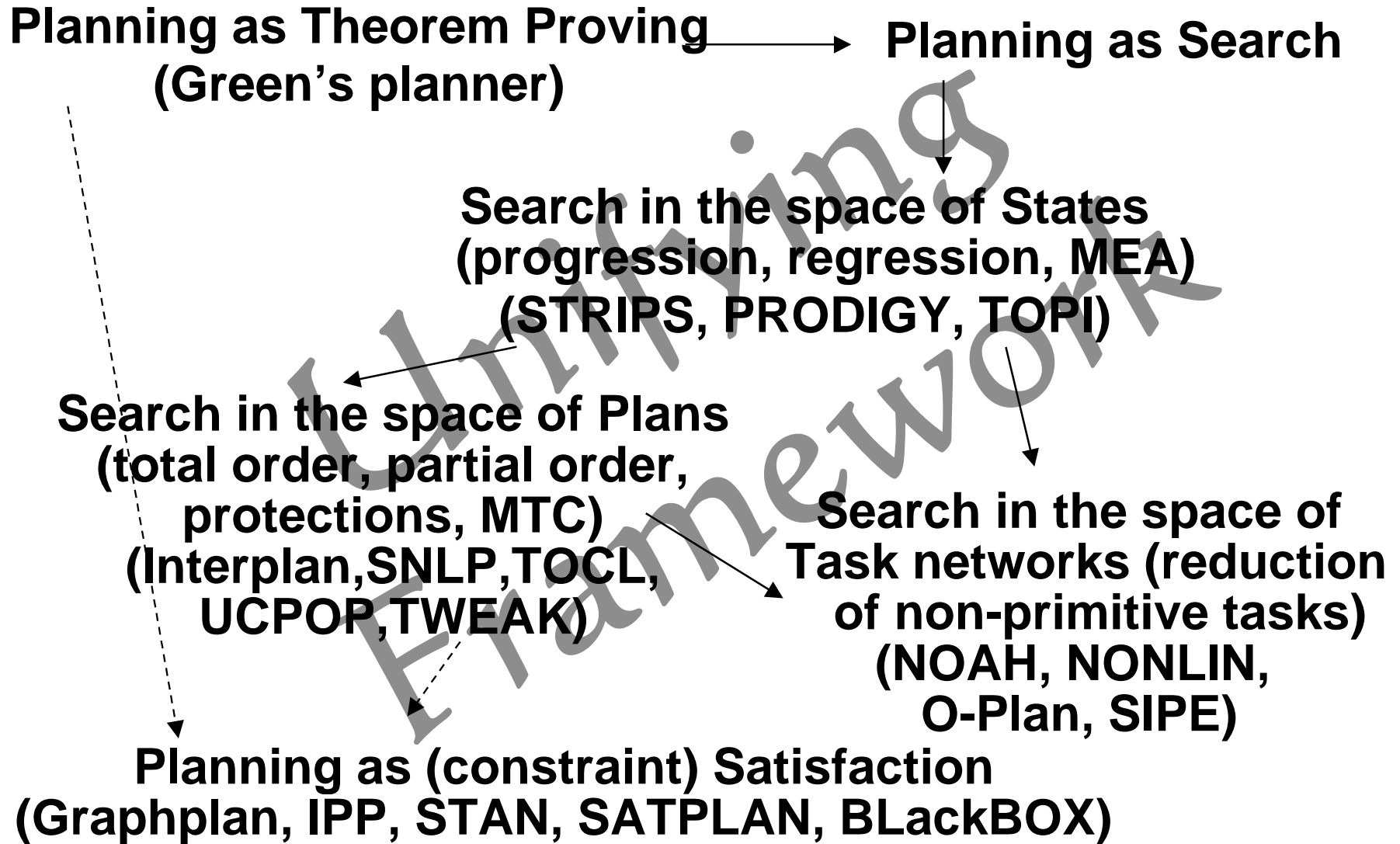
# Planning & (Classical Planning)



# Why care about classical Planning?

- ✧ **Many domains are approximately classical**
  - Stabilized environments
- ✧ **It is possible to handle near-classical domains through replanning and execution monitoring**
- ✧ **Classical planning techniques often shed light on effective ways of handling non-classical planning worlds**
  - Currently, most of the efficient techniques for handling non-classical scenarios are still based on ideas/advances in classical planning
- ✧ **Classical planning poses many interesting computational challenges**

# The (too) many brands of classical planners



# Advantages of the Unified View

**To the extent possible, this tutorial shuns brand names and reconstructs important ideas underlying those brand names in a rational fashion**

- ✧ **Better understanding of existing planners**
  - Normalized comparisons between planners
  - Evaluation of trade-offs provided by various design choices
- ✧ **Design of novel planning algorithms**
  - Hybrid planners using multiple refinements
  - Explication of the connections between planning, CSP, SAT and ILP



# Modeling Classical Planning: Actions, States, Correctness

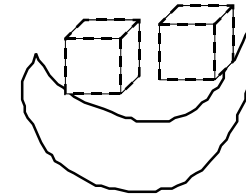
# Modeling Classical Planning

✧ States are modeled in terms of (binary) state-variables

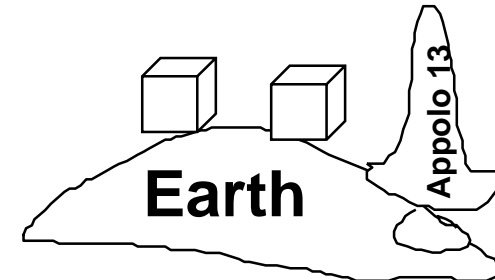
-- Complete initial state, partial goal state

✧ Actions are modeled as state transformation functions

-- Syntax: ADL language (Pednault)  
 -- Apply(A,S) = (S \ eff(A)) + eff(A)  
 (If Precond(A) hold in S)

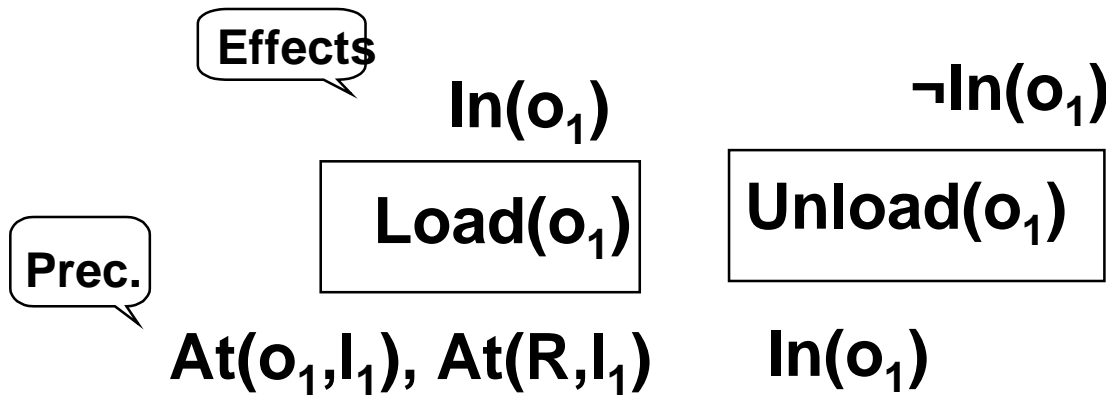


At(A,M), At(B,M)  
 $\neg$ In(A),  $\neg$ In(B)



At(A,E), At(B,E), At(R,E)

At(R,M),  $\neg$ At(R,E)  
 $\forall x \text{In}(x) \Rightarrow \text{At}(x, M) \ \& \ \neg \text{At}(x, E)$   
 Fly()  
 At(R,E)

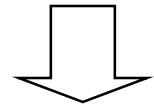


# Some notes on action representation

- ✧ **STRIPS Assumption: Actions must specify all the state variables whose values they change...**
- ✧ **No disjunction allowed in effects**
  - **Conditional effects are NOT disjunctive**
    - » (antecedent refers to the previous state & consequent refers to the next state)
- ✧ **Quantification is over finite universes**
  - **essentially syntactic sugaring**
- ✧ **All actions can be compiled down to a canonical representation where preconditions and effects are propositional**
  - **Exponential blow-up may occur (e.g removing conditional effects)**
    - » We will assume the canonical representation

Action A

Eff: If P then R  
If Q then W



Action A1  
Prec: P, Q  
Eff: R, W

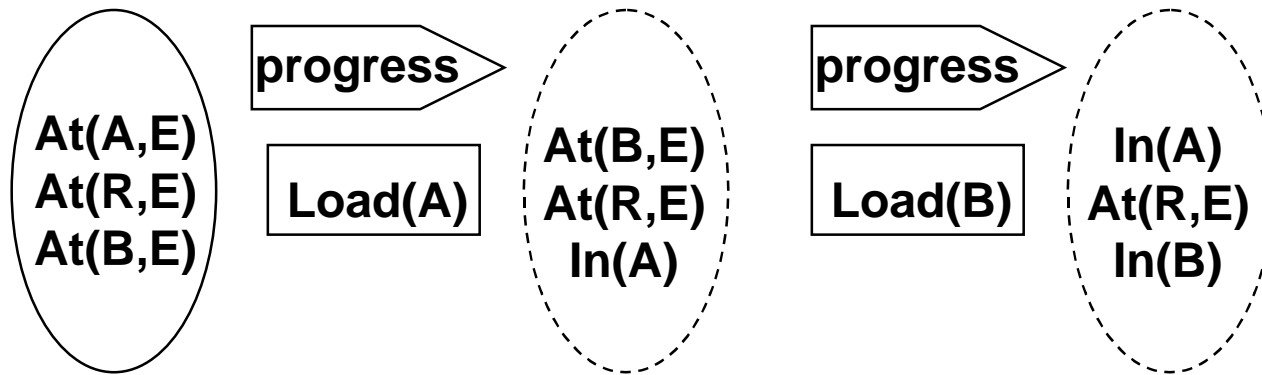
Action A2  
Prec: P, ~Q  
Eff: R, ~W

Action A3  
Prec: ~P, Q  
Eff: ~R, W

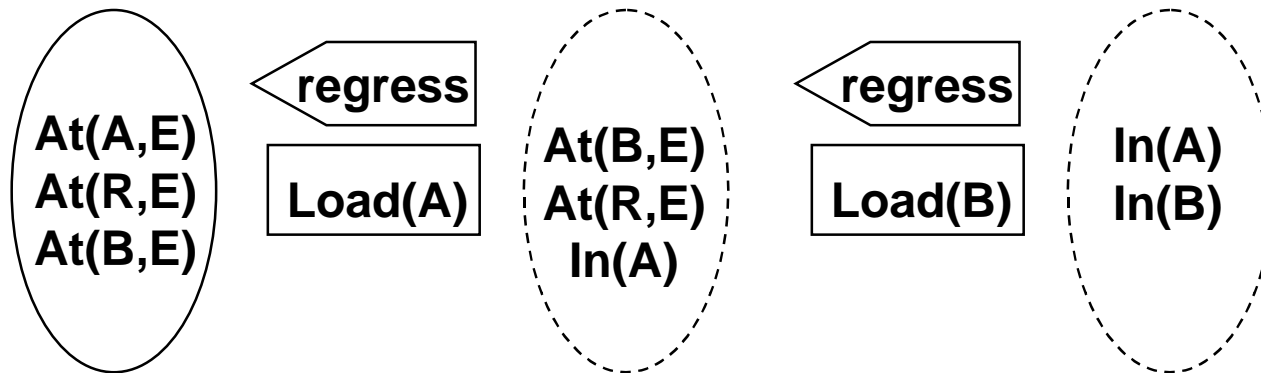
Action A4  
Prec: ~P, ~Q  
Eff:

# Checking correctness of a plan: The State-based approaches

- Progression Proof: Progress the initial state over the action sequence, and see if the goals are present in the result



- Regression Proof: Regress the goal state over the action sequence, and see if the initial state subsumes the result



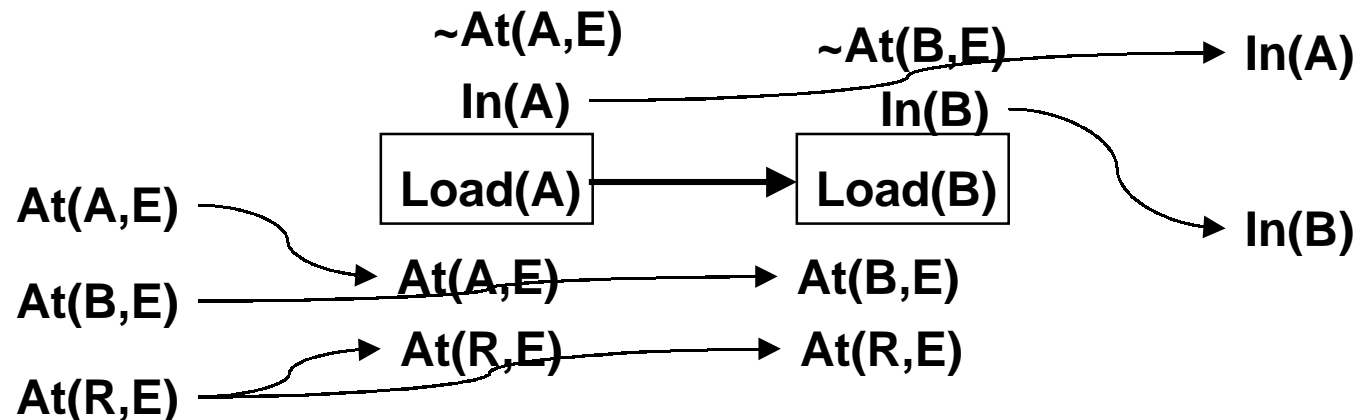
# Checking correctness of a plan: The Causal Approach

Contd..

- ✧ **Causal Proof:** Check if each of the goals and preconditions of the action are
  - » “established” : There is a preceding step that gives it
  - » “declobbered”: No possibly intervening step deletes it
    - Or for every preceding step that deletes it, there exists another step that precedes the conditions and follows the deleter adds it back.

## Causal proof is

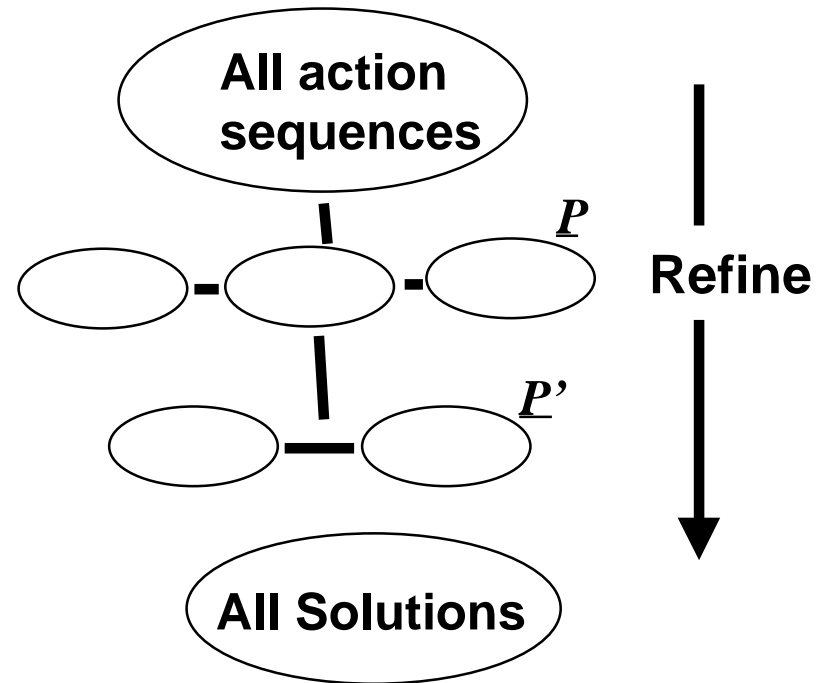
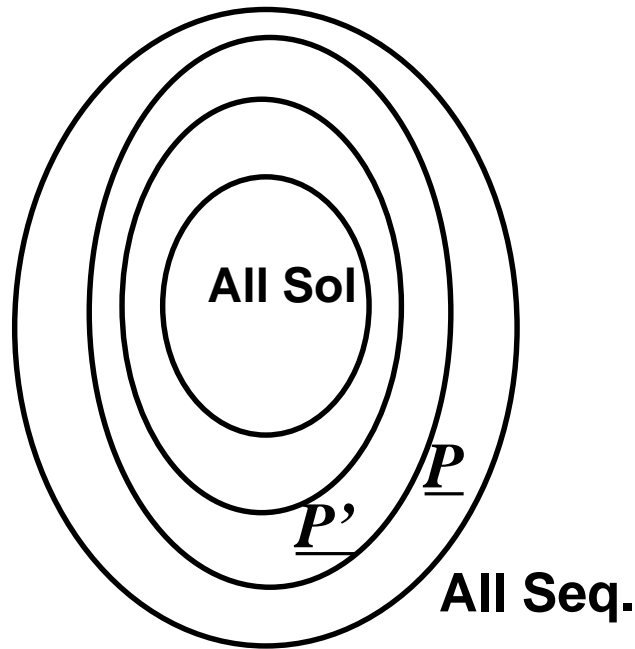
- “local” (checks correctness one condition at a time)
- “state-less” (does not need to know the states preceding actions)
- “incremental” with respect to action insertion



# The Refinement Planning Framework:

1. Syntax & Semantics of partial plans
2. Refinement strategies & their properties
3. The generic Refinement planning template

# Refinement Planning: Overview



Refinements

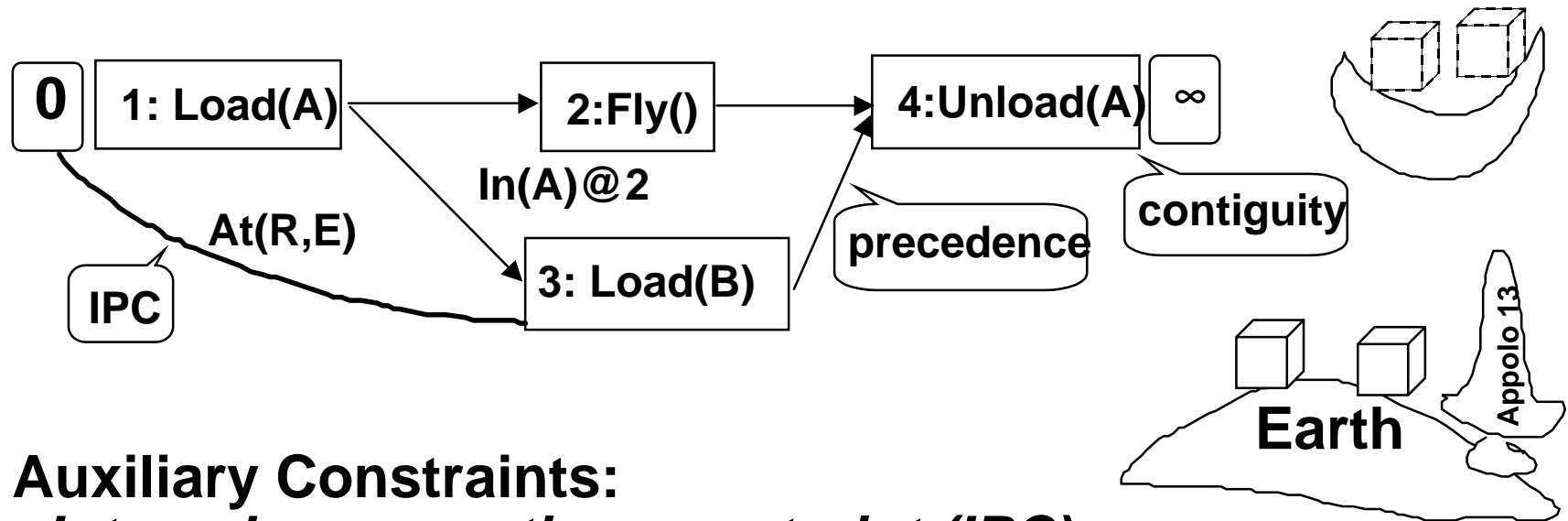
Partial plans

**Narrowing sets of action sequences  
to progress towards solutions**

Remove non-solutions

# Partial Plans: Syntax

Partial plan =  $\langle \text{Steps, Orderings, Aux. Constraints} \rangle$



## Auxiliary Constraints:

**Interval preservation constraint (IPC)**  $\langle s_1, p, s_2 \rangle$   
 $p$  must be preserved between  $s_1$  and  $s_2$

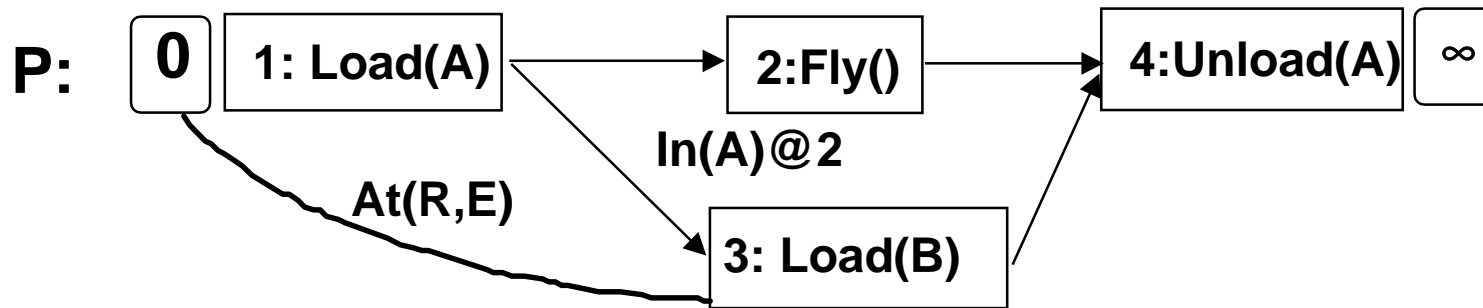
**Point truth Constraint (PTC)**  $p@s$   
 $p$  must hold in the state before  $s$



# Partial Plans: Semantics

Candidate is any action sequence that

- contains actions corresponding to all the steps,
- satisfies all the ordering and auxiliary constraints



Candidates ( $\in$  «P»)

Non-Candidates ( $\notin$  «P»)

[Load(A),Load(B),Fly(),Unload(A)]

Minimal candidate. Corresponds to safe linearization [ 01324 ∞ ]

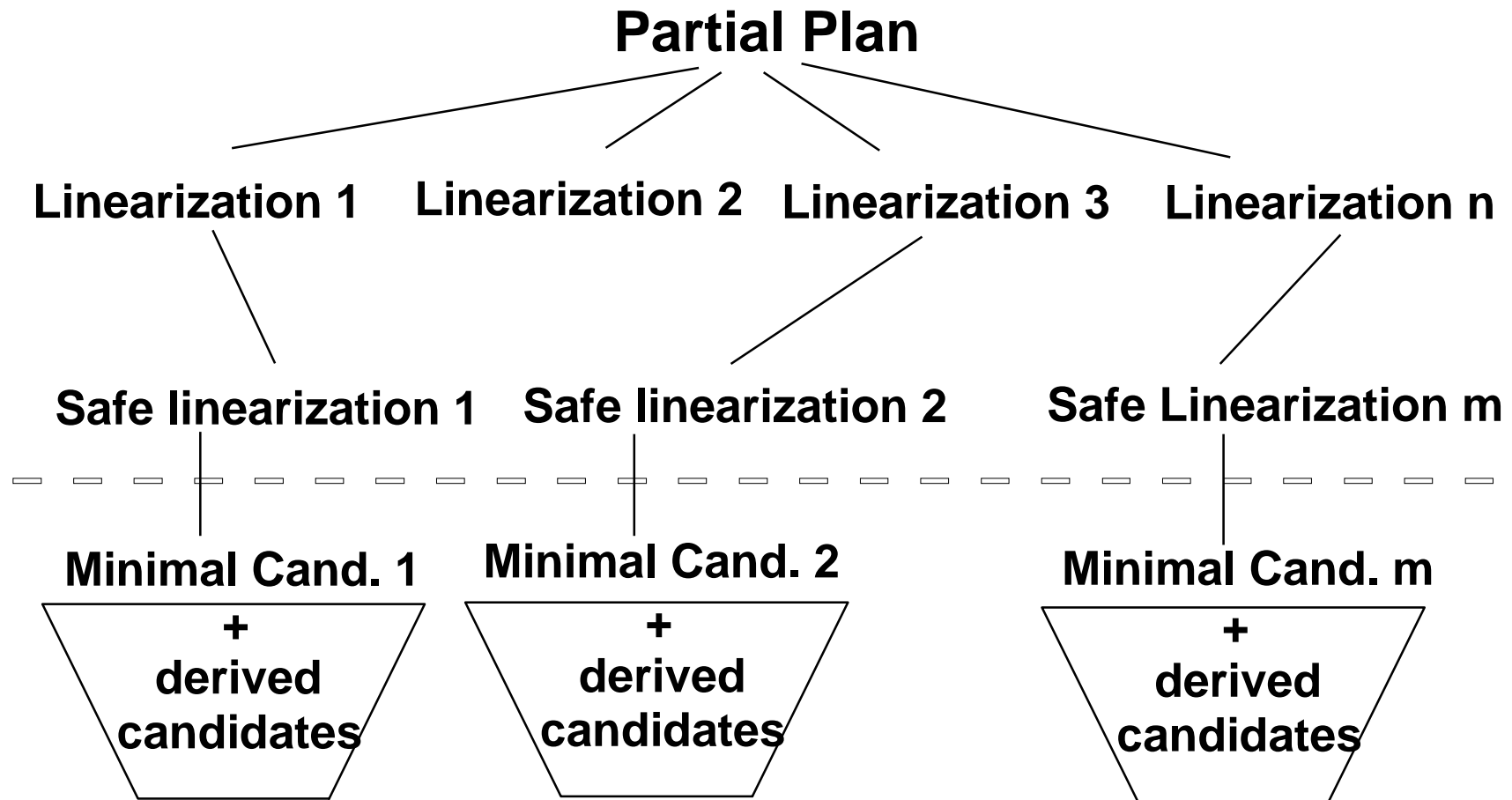
[Load(A),Load(B),Fly(),  
Unload(B),Unload(A)]

[Load(A),Fly(),Load(B),Unload(B)]

Corresponds to unsafe linearization [ 01234 ∞ ]

[Load(A),Fly(),Load(B),  
Fly(),Unload(A)]

# Linking Syntax and Semantics



**Refinements** → Reduce candidate set size  
→ Increase length of minimal candidates

# Refinement (pruning) Strategies

“Canned” inference procedures

actions & their inter-relations

-- Prune by propagating the consequences of domain theory and meta-theory of planning onto the partial plan

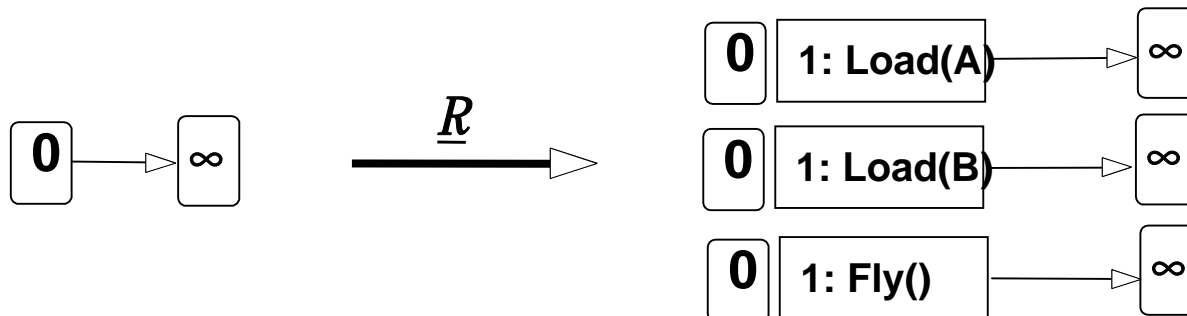
✧ A refinement strategy  $\underline{R} : \underline{P} \rightsquigarrow \underline{P}'$  ( « $\underline{P}'$ » a subset of « $\underline{P}$ » )

– $\underline{R}$  is complete if « $\underline{P}'$ » contains all the solutions of « $\underline{P}$ »

– $\underline{R}$  is monotonic if « $\underline{P}'$ » has longer minimal candidates than « $\underline{P}$ »

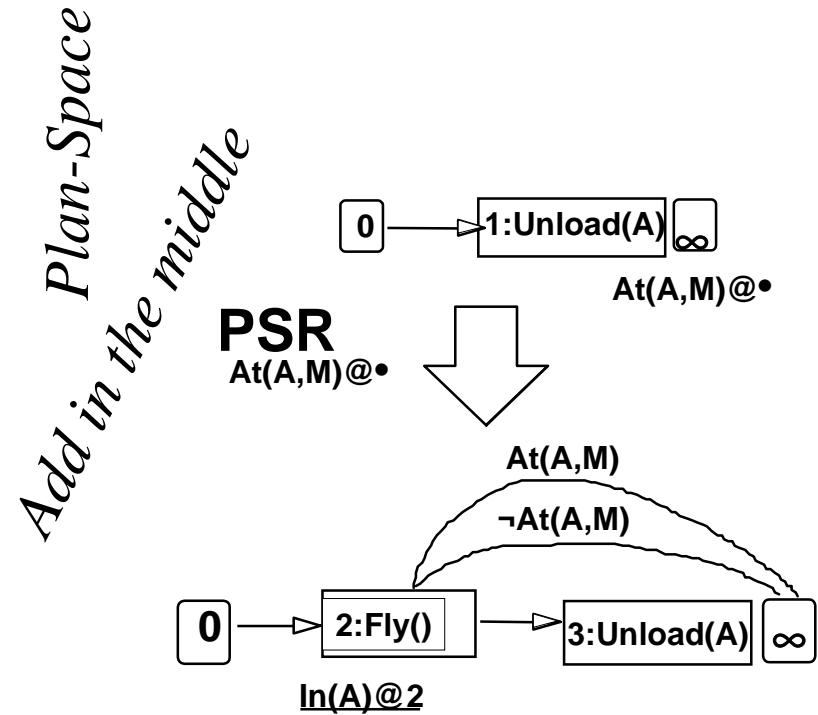
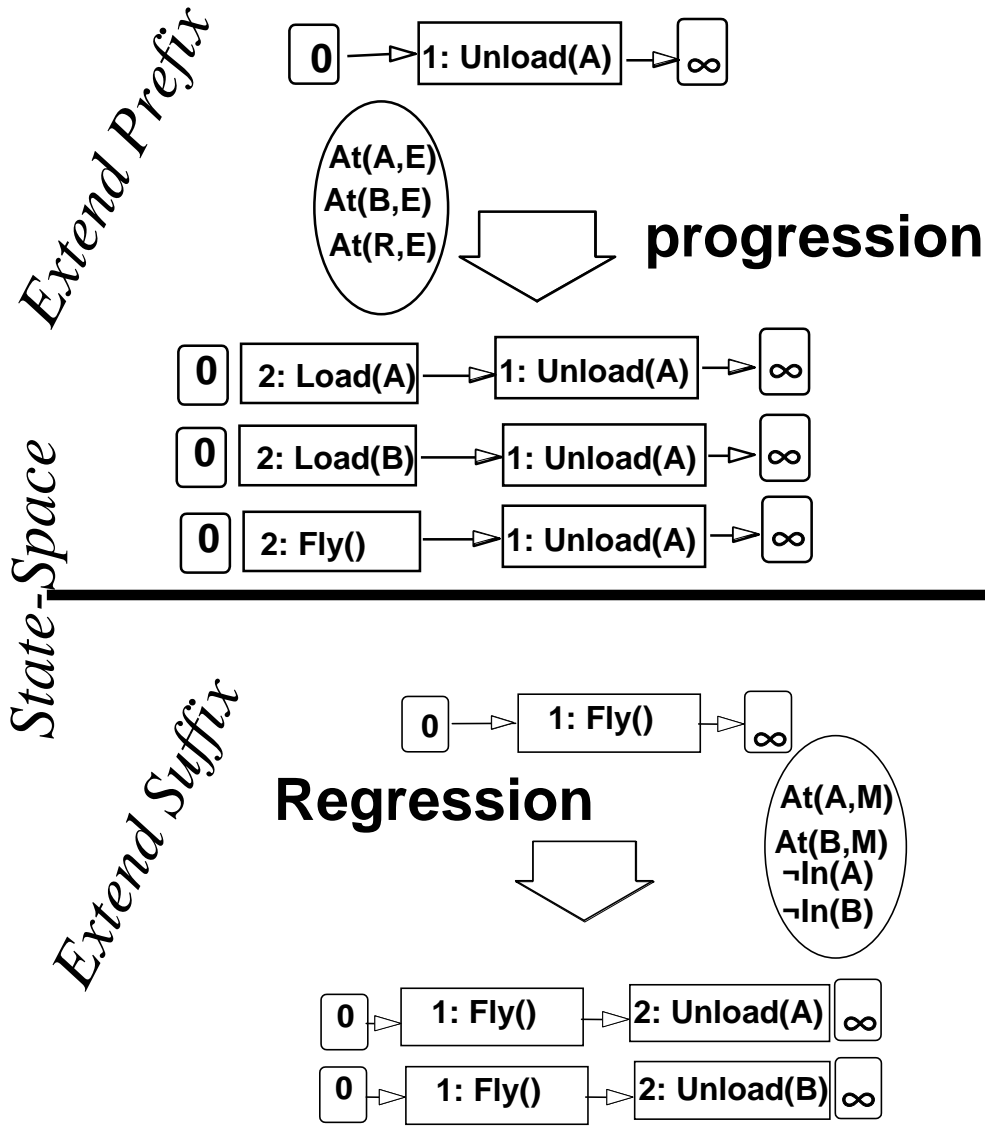
– $\underline{R}$  is progressive if « $\underline{P}'$ » is a proper subset of « $\underline{P}$ »

– $\underline{R}$  is systematic if components of  $\underline{P}'$  don't share candidates

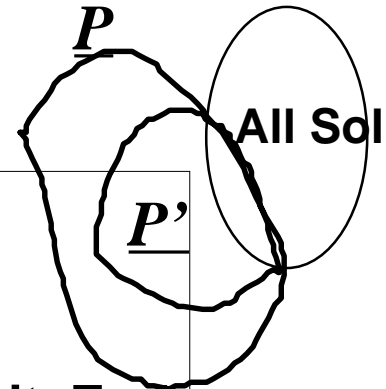


§ A plan set  $\underline{P}$  is a set of partial plans  $\{P_1, P_2 \dots P_m\}$

# Existing Refinement Strategies



# The Refinement Planning Template



Refineplan(  $\underline{P}$  : Plan set)

0\*. If « $\underline{P}$ » is empty, Fail.

1. If a minimal candidate of  $\underline{P}$  is a solution, return it. End

2. Select a refinement strategy  $\underline{R}$

Apply  $\underline{R}$  to  $\underline{P}$  to get a new plan set  $\underline{P}'$

3. Call Refine( $\underline{P}'$ )

-- Termination ensured if  $\underline{R}$  is complete and monotonic

-- Solution check done using one of the proofs of correctness

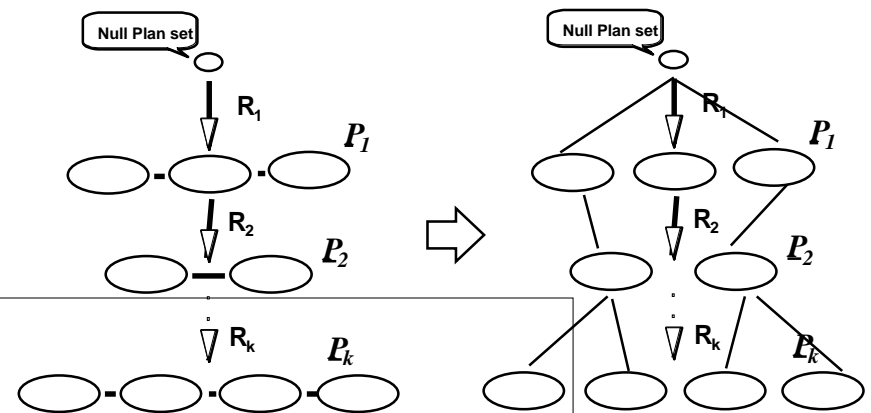
Issues:

1. Representation of plan sets (Conjunctive vs. Disjunctive)

2. Search vs. solution extraction

3. Affinity between refinement and proof used for solution check

# A flexible Split&Prune search for refinement planning



## Refineplan(P : Plan)

- 0\*. If «P» is empty, Fail.
1. If a minimal candidate of P is a solution, terminate.
2. Select a refinement strategy R.  
Apply R to P to get a new plan set P'
3. Split P' into k plansets
4. Non-deterministically select one of the plansets P'<sub>i</sub>  
Call Refine(P'<sub>i</sub>)

# Two classes of refinement planners

*Then*

## *Conjunctive planners*

- ◇ **Search in the space of conjunctive partial plans**
  - Disjunction split into the search space
    - » search guidance is nontrivial
  - Solution extraction is trivial
- ◇ **Examples:**
  - STRIPS & Prodigy
  - SNLP & UCPOP
  - NONLIN & SIPE
  - UNPOP & HSP

*Now*

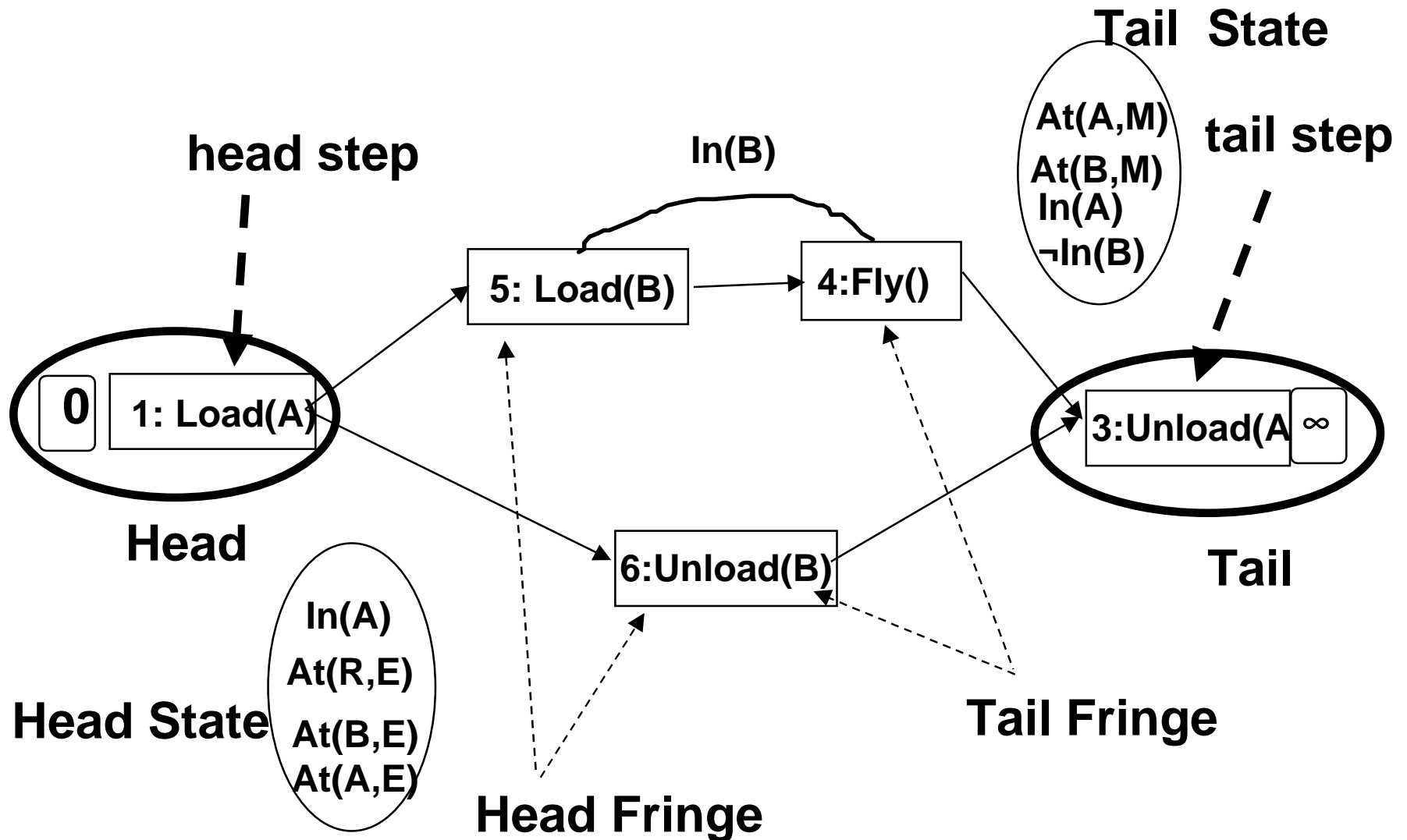
## *Disjunctive planners*

- ◇ **Search in the space of disjunctive partial plans**
  - Disjunction handled explicitly
  - Solution extraction is non-trivial
    - » CSP/SAT/ILP methods
- ◇ **Examples:**
  - Graphplan
  - SATPLAN

# CONJUNCTIVE REFINEMENT PLANNING

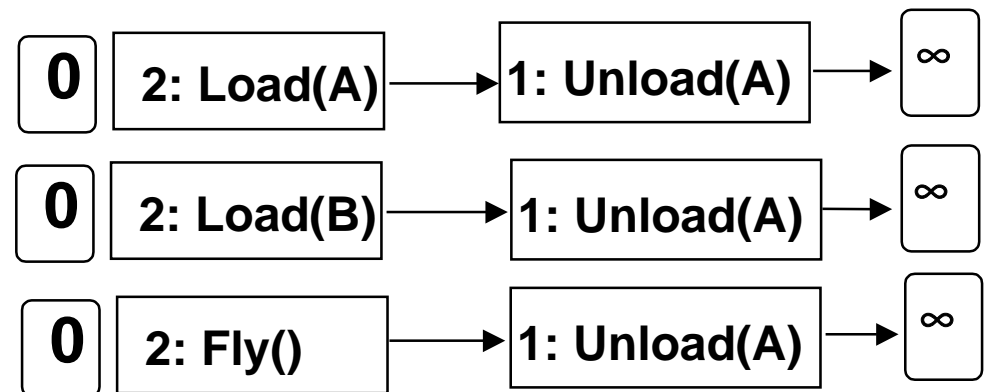
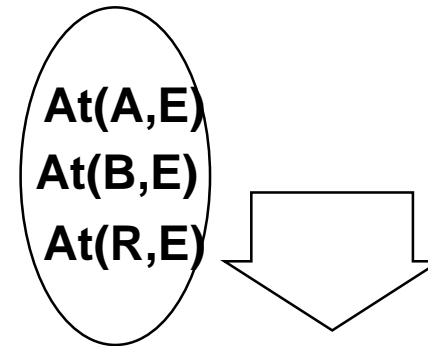


# Plan structure nomenclature



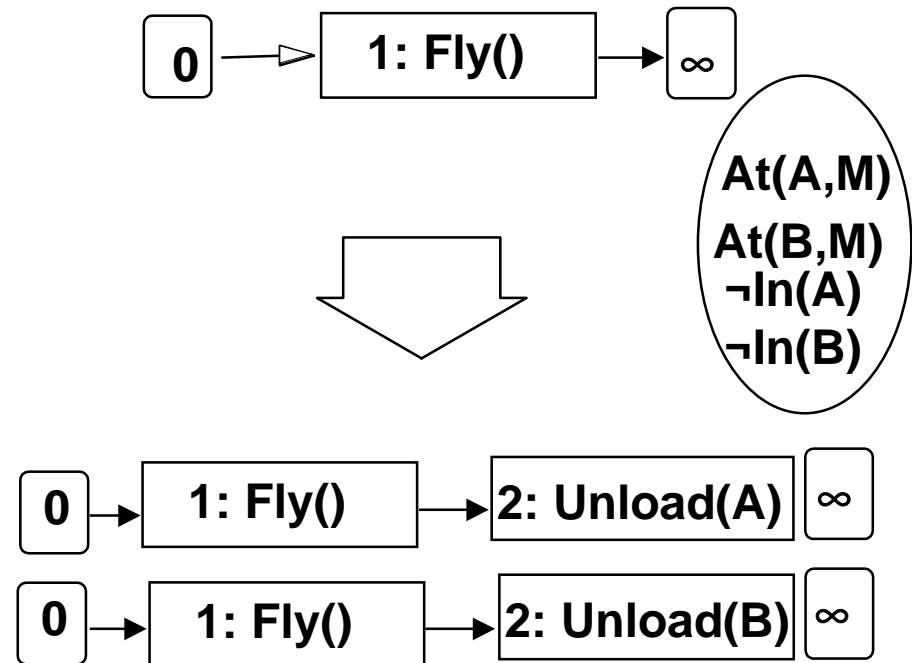
# Forward State-space Refinement

- ✧ **Grow plan prefix by adding applicable actions**
  - Complete, Monotonic
    - » *consideration of all executable prefixes*
  - Progressive
    - » *elimination of unexecutable prefixes*
  - Systematic
    - » *each component has a different prefix*
- ✚ **Completely specified state**
  - » **Easier to control?**



# Backward State-space Refinement

- ◇ Grow plan suffix by adding relevant actions
  - Complete, Monotonic
    - » *consideration of all relevant suffixes*
  - Progressive
    - » *elimination of irrelevant suffixes*
  - Systematic
    - » *each component has a different suffix*
- ⊕ Goal directed
  - » Lower branching



# Plan-space Refinement

**Goal selection:**

Select a precondition

**Establishment:**

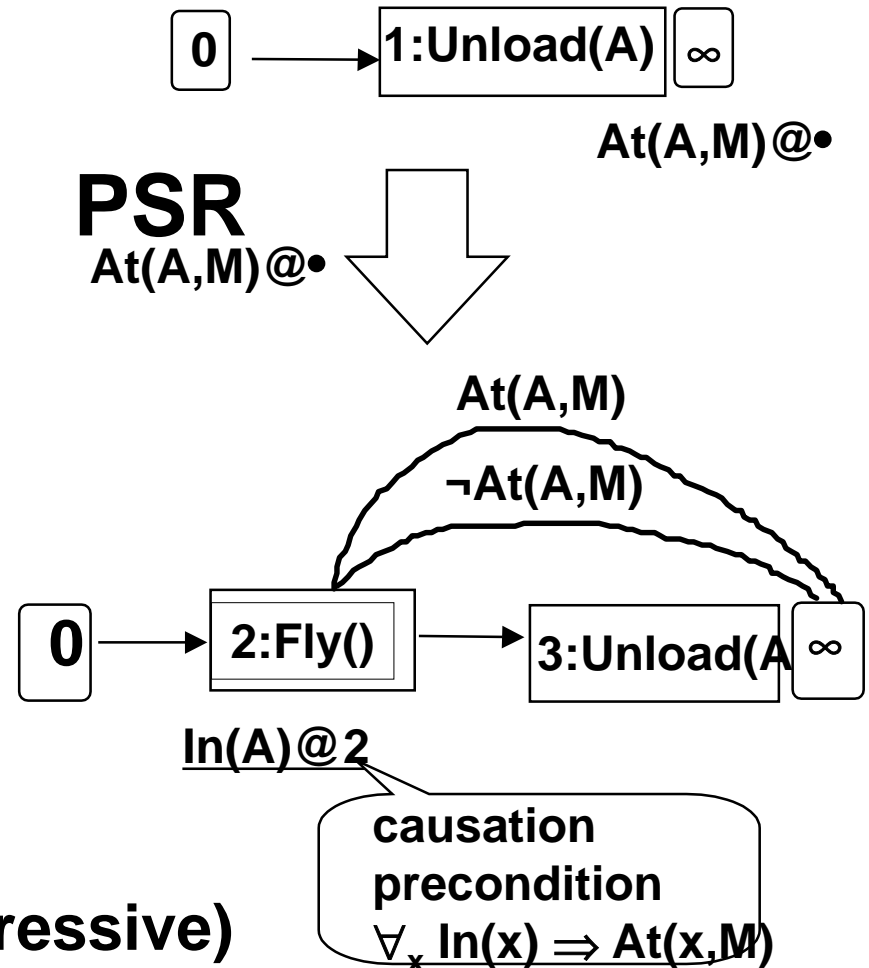
Select a step (new or existing) and make it give the condition

**De-clobbering:**

Force intervening steps to preserve the condition

**Book-keeping: (Optional)**

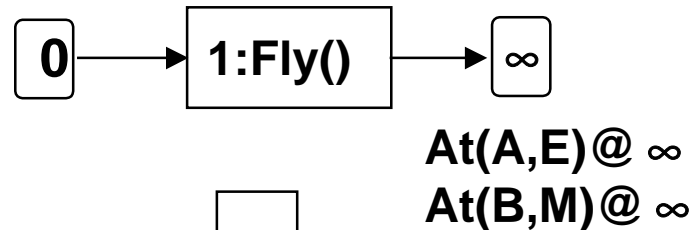
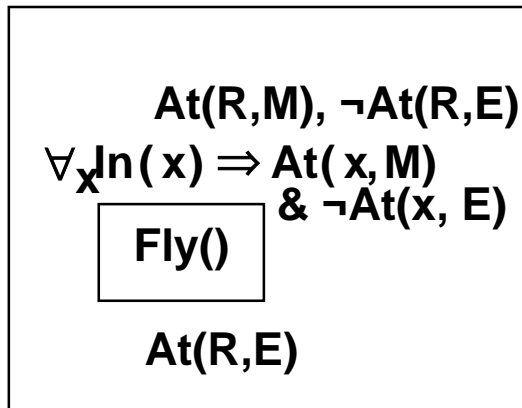
Add IPCs to preserve the establishment  
 $\Rightarrow$  Systematicity



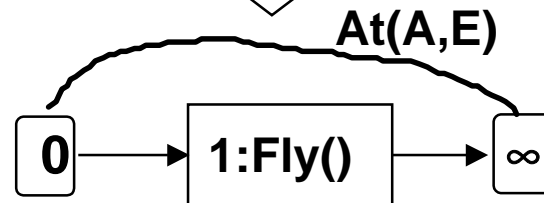
**(PSR is complete, and progressive)**

*(Sacerdoti, 1972; Pednault, 1988; McAllester, 1991)*

# Plan-space Refinement: Example 2



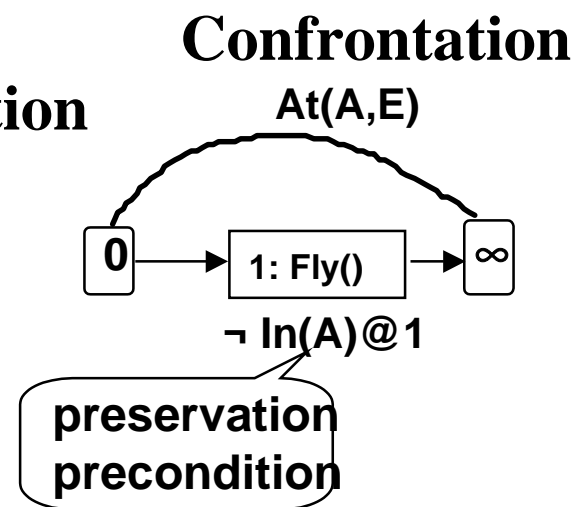
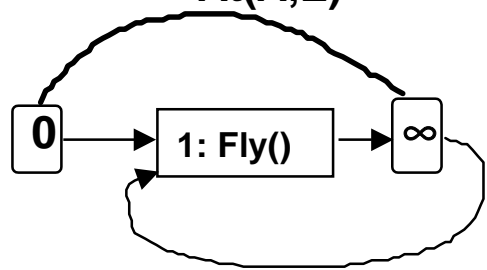
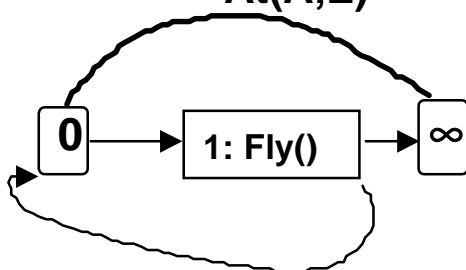
**Establishment**  
 $At(A,E)@ \infty$



**Arbitration**

**Promotion**      **Demotion**

$At(A,E)$        $At(A,E)$

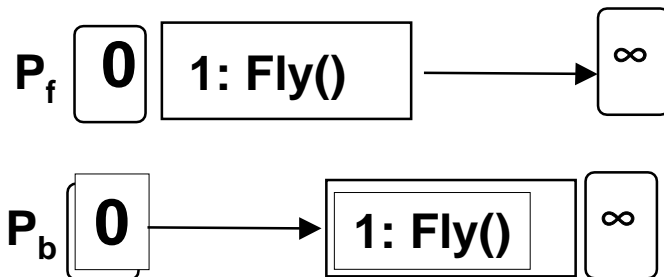


# Position, Relevance and Commitment

The Tastes great/  
Less Filling debate

FSR and BSR must commit to both position and relevance of actions

- + Gives state information
- Leads to premature commitment



Plan-space refinement (PSR) avoids constraining position

- + Reduces commitment
- Increases plan-handling costs



# Generating Conjunctive Refinement Planners

## Refineplan ( $\underline{P}$ : Plan)

0\*. If « $\underline{P}$ » is empty, Fail.

1. If a minimal candidate of  $\underline{P}$  is a solution, terminate.

2. Select a refinement strategy  $\underline{R}$ .

Apply  $\underline{R}$  to  $\underline{P}$  to get a set of new plans  $\underline{P}_1 \dots \underline{P}_j$

Add all plans to the search queue.

4. Non-deterministically select one of the plans  $\underline{P}_i$   
Call Refine( $\underline{P}_i$ )

Keep all linearizations safe  
(Tractability refinements)  
Select the proof strategy so it becomes  
incremental with respect to the refinement  
Stick to a single refinement strategy

# Issues in instantiating Refineplan

- ✧ **Although a planner can use multiple different refinements, most implementations stick to a single refinement**
- ✧ **Although refinement can be used along with any type of correctness check, there is affinity between specific refinements and proof techniques (support finite differencing)**
  - **FSR and Progression based proof**
  - **BSR and Regression based proof**
  - **PSR and Causal proof**
- ✧ **Although it is enough to check if *any one* of the safe linearizations are solutions, most planners refine a partial plan until all its linearizations are safe**
  - **Tractability refinements (pre-order, pre-satisfy)**

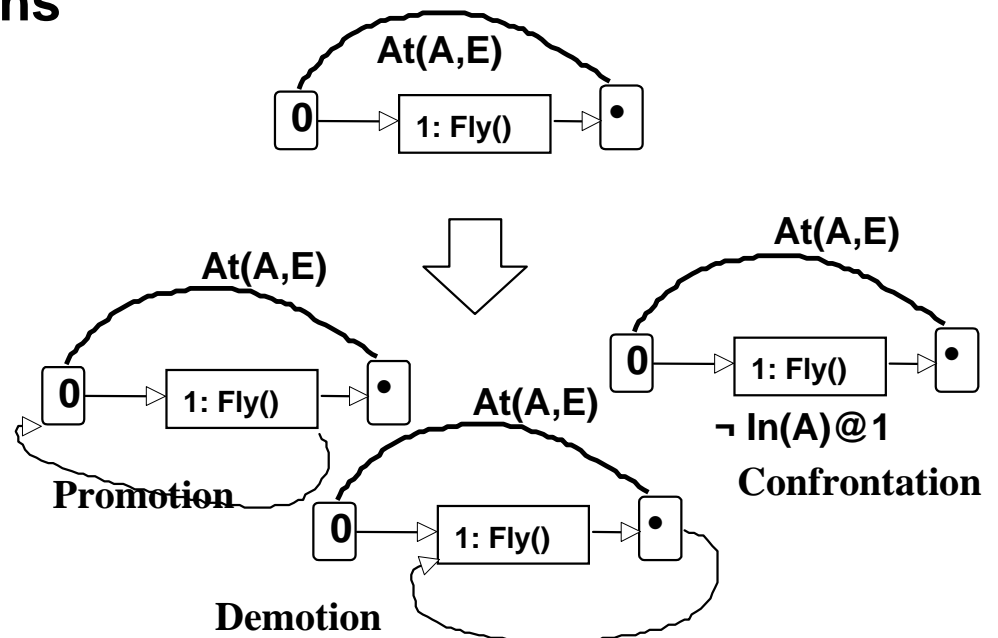
With these changes, an instantiated and simplified planner may “*look*” considerably different from the general template



# Tractability Refinements

*Aim: Make it easy to generate minimal candidates*

- ◇ Reduce number of linearizations
  - Pre-ordering
  - Pre-positioning
- ◇ Make all linearizations safe
  - Pre-satisfaction
    - » Resolve threats to auxiliary constraints
- ◇ Reduce uncertainty in action identity
  - Pre-reduction
    - » Replace a non-primitive action with its reductions



# Case Study: UCPOP

## Refineplan ( $\underline{P}$ : Plan)

- 0\*. If  $P$  is order inconsistent, FAIL.
- 1. If no open conditions and no unsafe IPCs, SUCCESS.
- 2. Generate new plans using either 2' or 2''  
Add the plans to the search queue
- 2'. Remove an open condition  $c@s$  in  $P$ .
  - 2.1. For each step  $s'$  in  $P$  that gives  $c$ , make a new plan  
 $P' = P + (s' < s) + \text{IPC } s'-c-s$
  - 2.2. For each action  $A$  in the domain that gives  $c$ , make a new plan  $P' = P + s_n:A + (s_n < s) + \text{IPC } s_n-c-s$ .
    - 2.2.1. For each precondition  $c'$  of  $A$ , add  $c'@s_n$  to the list of open conditions of  $P'$ .
    - 2.2.2. For each IPC  $s'-p-s''$ , if  $s_n$  deletes  $p$ , add  $[s'-p-s''; s_n]$  to the list of unsafe IPCs of  $P'$ .
- 2''. Remove an unsafe IPC  $[s'-p-s''; s''']$  from  $P$ .  
Make two plans:  $P' = P + s''' < s'$   $P'' = P + s'' < s'''$
- 3. Non-deterministically select one of the plans  $P_i$  from the search queue and Call Refine( $\underline{P}_i$ )

Incremental  
Soln. check

Finite-differencing  
structures

Tractability  
refinement

# Many variations on the theme..

<i>Planner</i>	<i>Termination</i>	<i>Goal Sel.</i>	<i>Bookkeeping</i>	<i>Tractability refinements</i>
TWEAK	MTC	MTC	-none-	-none-
UA	MTC	MTC	-none-	pre-order
SNLP / UCPOP	Causal proof	arbitrary	Contrib. Prot	pre-satisfaction
TOCL	Causal proof	arbitrary	Contrib. Prot.	pre-order
McNonlin/ Pedestal	Causal proof	arbitrary	Interval Prot.	pre-satisfaction
SNLP-UA	MTC	MTC	Contrib. Prot.	unambig. ord.

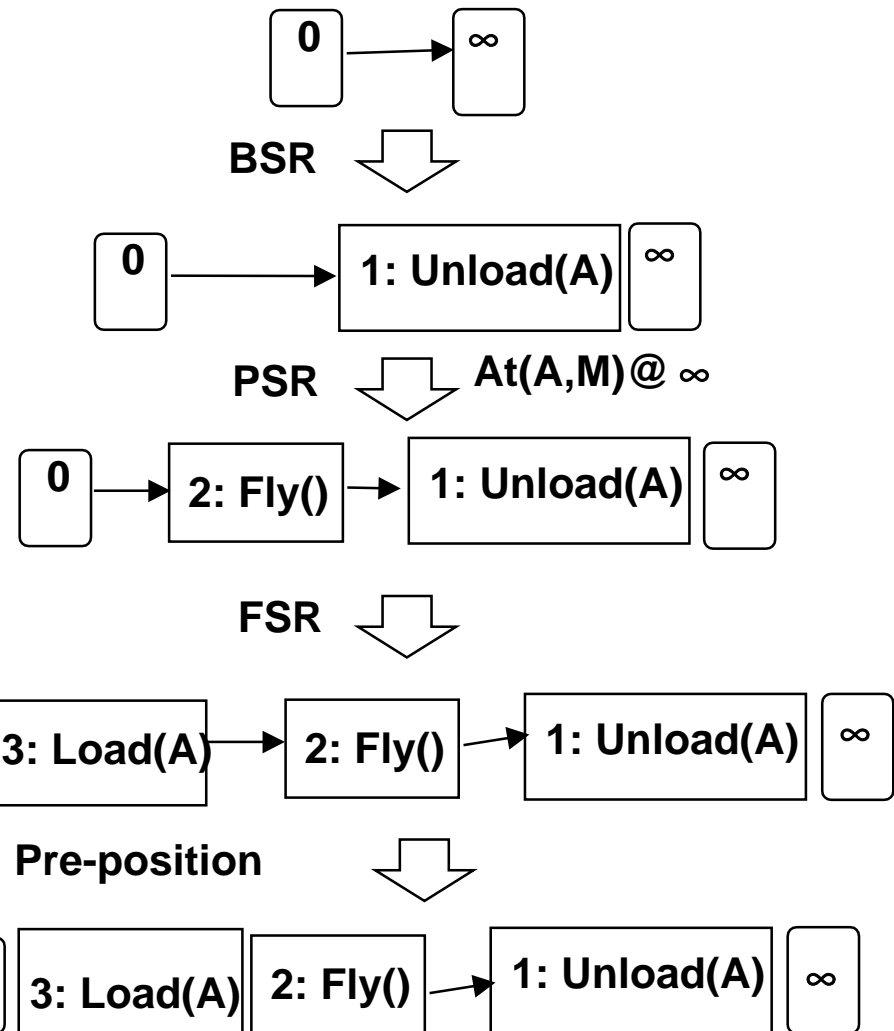
*(Kambhampati, Knoblock & Yang, 1995)*

# Interleaving Refinements

- ✧ **Combine different refinements opportunistically**
  - Can be more efficient than single-refinement planners
  - Refinement selection criteria?

» # Components produced

» “Progress” made



(Kambhampati & Srivastava, 1995)

# Effective Heuristics for conjunctive planners

- ✧ **State-space planners can be focused with greedy regression graphs (see below)**
- ✧ **Plan-space planners are focused by “flaw selection” strategies**
  - **Select the flaw (open condition, unsafe IPC) that has the fewest number of resolution possibilities**
    - » **(Fail first heuristic)**
  - **Maintain the live resolution possibilities for each flaw (Descartes)**
    - » **(Forward Checking)**

# Greedy Regression Graphs

**Problem:** Estimate the length of the plan needed to go from the head-state of the current partial plan to the goal state.

**Solution:** --Relax the problem by assuming that all subgoals are independent (ignore +ve / -ve interactions between actions)  
--Solve the relaxed problem and use the length of the solution as part of the heuristic

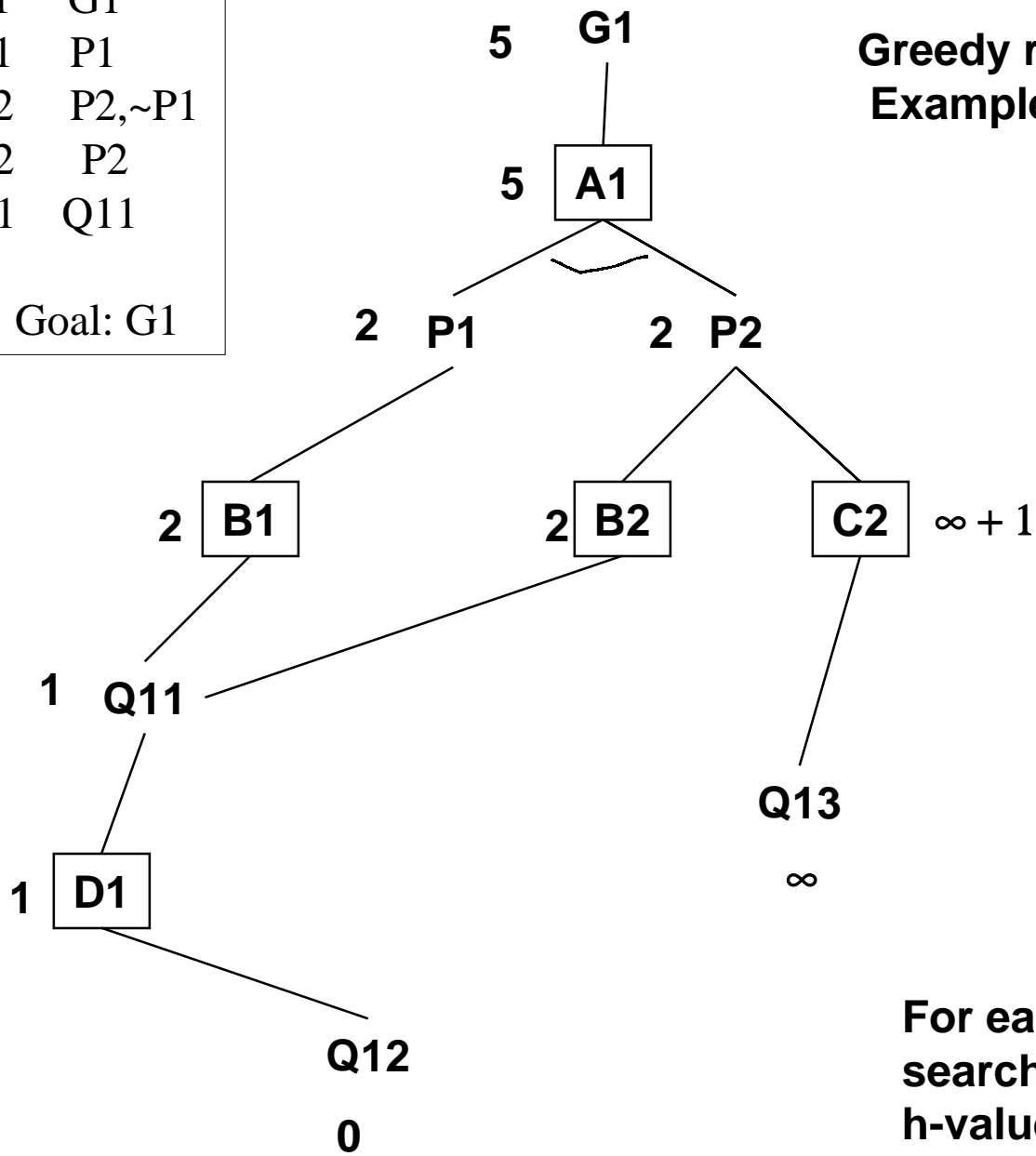
**Properties:** The heuristic is neither a lower bound (-ve interactions) nor an upper-bound (+ve interactions).  
--leads to inoptimal solutions (in terms of plan length)  
>>Possible to reduce inoptimality by considering interactions

The heuristic can also be made to work in the reverse direction

**Planners:** UNPOP (McDermott); HSP (Bonet & Geffner)

P1,P2	A1	G1
Q11	B1	P1
Q11	B2	P2,~P1
Q13	C2	P2
Q12	D1	Q11

Init: Q12 Goal: G1



**Greedy regression Graph:  
Example**

*+ve as well as  
-ve interactions  
between P1 and P2  
are ignored....*

**For each partial plan in the  
search queue, estimate its  
h-value using this procedure**

## Some implemented conjunctive planners

	Refinement	Heuristics
<b>UCPOP, SNLP</b> [Weld et. al. ]	<b>Plan-space</b>	<b>Fail-first</b> <b>Flaw selection</b>
<b>UNPOP [McDermott]</b> <b>HSP [Geffner &amp; Bonet]</b>	<b>Forward state space</b>	<b>Greedy regression</b>
<b>Descartes</b> [Joslin & Pollack] <b>UCPOP-D</b> [Kambhampati & Yang]	<b>Plan-space</b>	<b>Forward checking +</b> <b>Fail-first flaw selection</b>
<b>Prodigy</b> [Carbonell et. al. ]	<b>Forward state space</b>	<b>Means-ends analysis</b>



# Conjunctive planners: The State of the Art

- ✧ **Vanilla state-space (FSR/BSR) planners were known to be less efficient than vanilla plan-space planners**
  - **Several research efforts concentrated on extending plan-space approaches to non-classical scenarios**
- ✧ **Forward state-space planners using greedy regression heuristic are competitive with the best available planners**
  - **At this time, there do not seem to be comparably effective heuristics for plan-space planners.**
- ✧ **Plan-space planners still provide better support for incremental planning (replanning, reuse and plan modification)**

# DISJUNCTIVE REFINEMENT PLANNING

# Disjunctive Planning

- ✧ **Idea: Consider Partial plans with disjunctive step, ordering, and auxiliary constraints**
- ✧ **Motivation: Provides a lifted search space, avoids re-generating the same failures multiple times (also, rich connections to combinatorial problems)**
- ✧ **Issues:**
  - **Refining disjunctive plans**
    - » **Graphplan (Blum & Furst, 95)**
  - **Solution extraction in disjunctive plans**
    - » **Direct combinatorial search**
    - » **Compilation to CSP/SAT/ILP**

***We will first review some core CSP/SAT concepts and then discuss approaches to disjunctive planning***

# CSP and SAT Review

# (very) Quick overview of CSP/SAT concepts

## ◇ Constraint Satisfaction Problem (CSP)

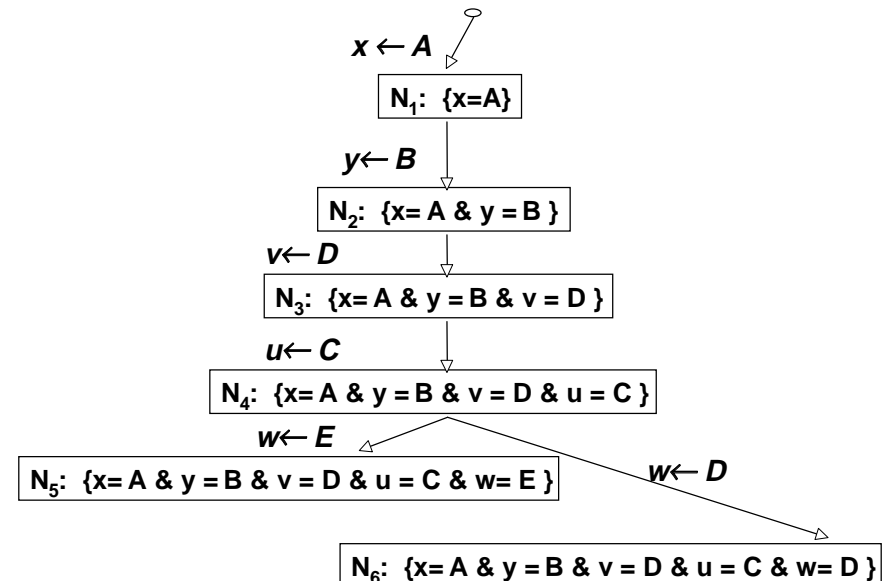
- Given
  - » A set of discrete variables
  - » Legal domains for each of the variables
  - » A set of constraints on values groups of variables can take
- Find an assignment of values to all the variables so that none of the constraints are violated

## ◇ SAT Problem = CSP with boolean variables

$x, y, u, v: \{A, B, C, D, E\}$   
 $w: \{D, E\} \mid \{A, B\}$   
 $x=A \Rightarrow w \neq E$   
 $y=B \Rightarrow u \neq D$   
 $u=C \Rightarrow l \neq A$   
 $v=D \Rightarrow l \neq B$

*A solution:*

$x=B, y=C, u=D, v=E, w=D, l=B$

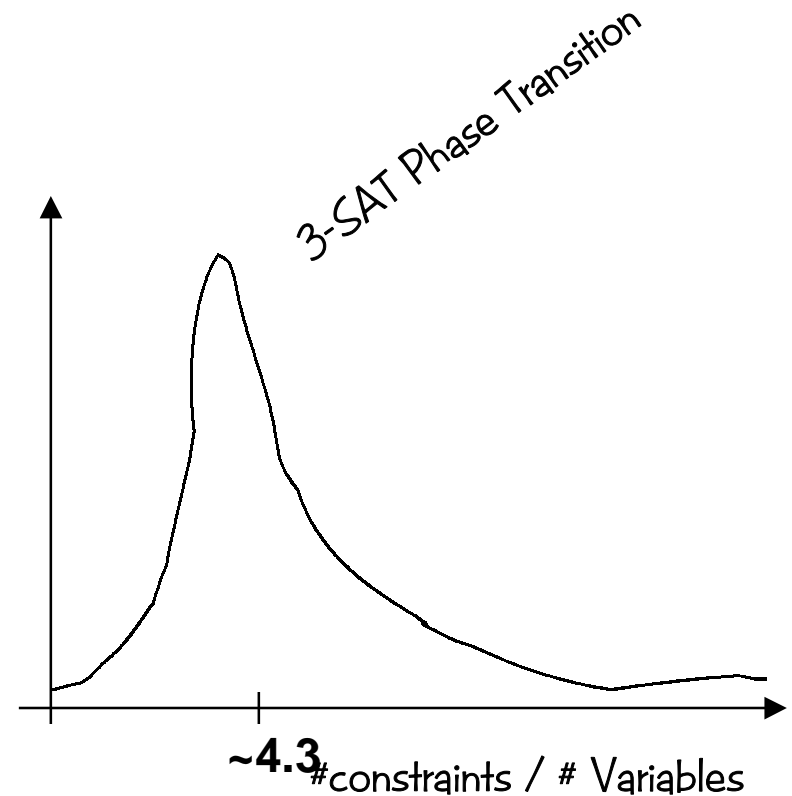


# What makes CSP problems hard?

Assignments to individual variables that seem locally consistent are often globally infeasible, causing costly backtracking.

The difficulty of a CSP/SAT problem depends on

- Number of variables (propositions)
- Number of constraints (clauses)
- Degree of local consistency



# Hardness & Local Consistency

- ✧ An n-variable CSP problem is said to be k-consistent iff every consistent assignment for (k-1) of the n variables can be extended to include any k-th variable
  - » Directional consistency: Assignment to first k-1 variables can be extended to the k-th variable
  - » Strongly k-consistent if it is j-consistent for all j from 1 to k
- ✧ Higher the level of (strong) consistency of problem, the lesser the amount of backtracking required to solve the problem
  - A CSP with strong n-consistency can be solved without any backtracking
- ✧ We can improve the level of consistency of a problem by explicating implicit constraints
  - Enforcing k-consistency is of  $O(n^k)$  complexity
    - » Break-even seems to be around k=2
    - » Use of directional and partial consistency enforcement techniques

# Important ideas in solving CSPs

## Variable order heuristics:

- Pick the variable with smallest domain
- Or the variable that constrains most other variables
- Or the variable that supports most unit propagation

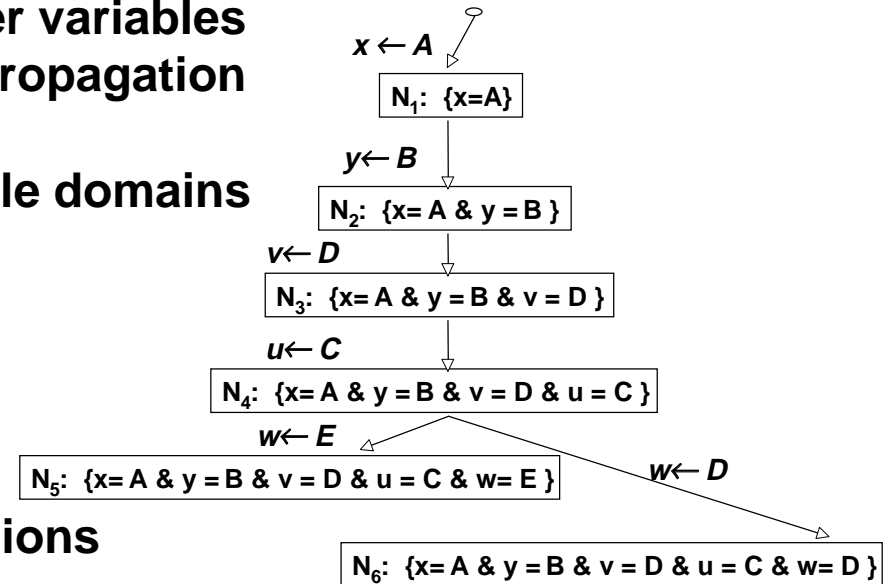
## Forward Checking: Filter out future variable domains based on current assignments

--Unit propagation fills this role in SAT

## DDB: Explain the failure at the dead-end nodes in terms of violated constraints, and during backtracking, skip over decisions that do not affect the explanation

## EBL: Remember interior node failure explanations as additional (implied) constraints)

## Local Search Methods: Change the assignment leading to most increase in the number of satisfied constraints



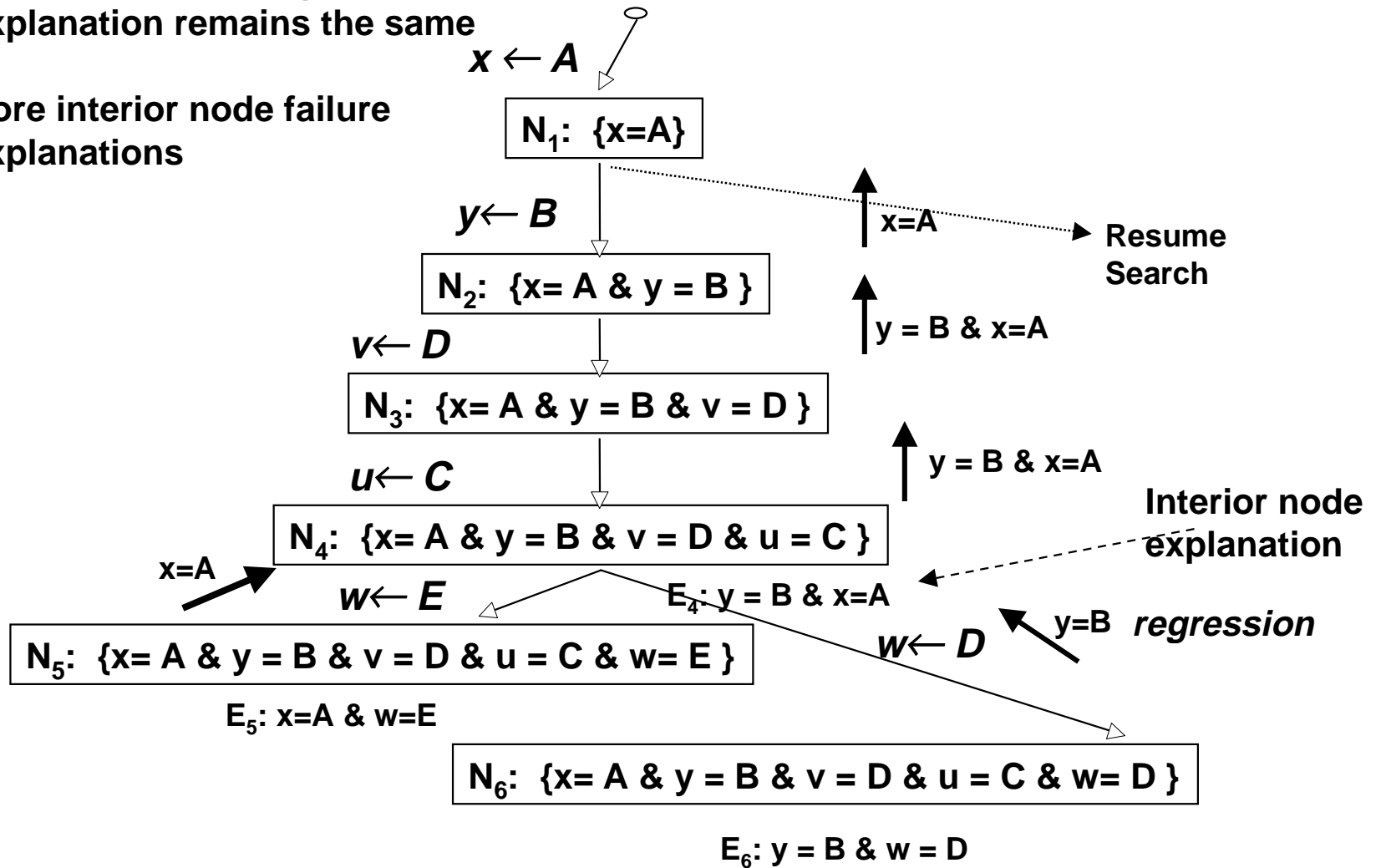
$x, y, u, v: \{A, B, C, D, E\}$   
 $w: \{D, E\} \quad l: \{A, B\}$   
 $x=A \Rightarrow w \neq E$   
 $y=B \Rightarrow u \neq D$   
 $u=C \Rightarrow l \neq A$   
 $v=D \Rightarrow l \neq B$



# DDB & EBL

**DDB: Skip a level if the regressed Explanation remains the same**

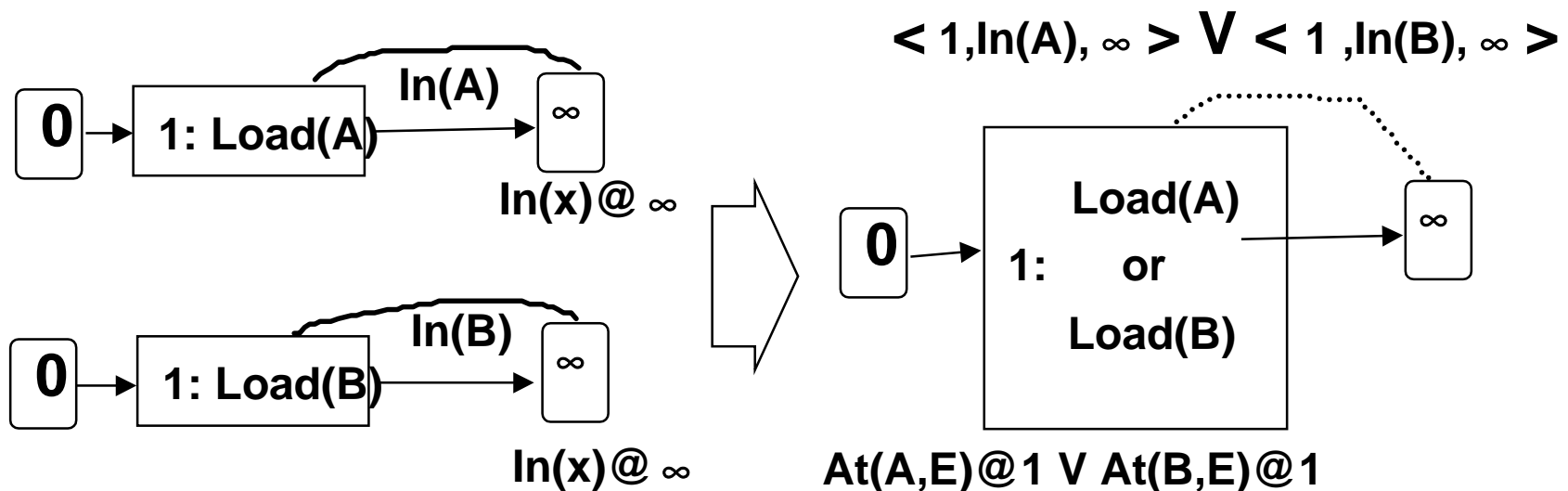
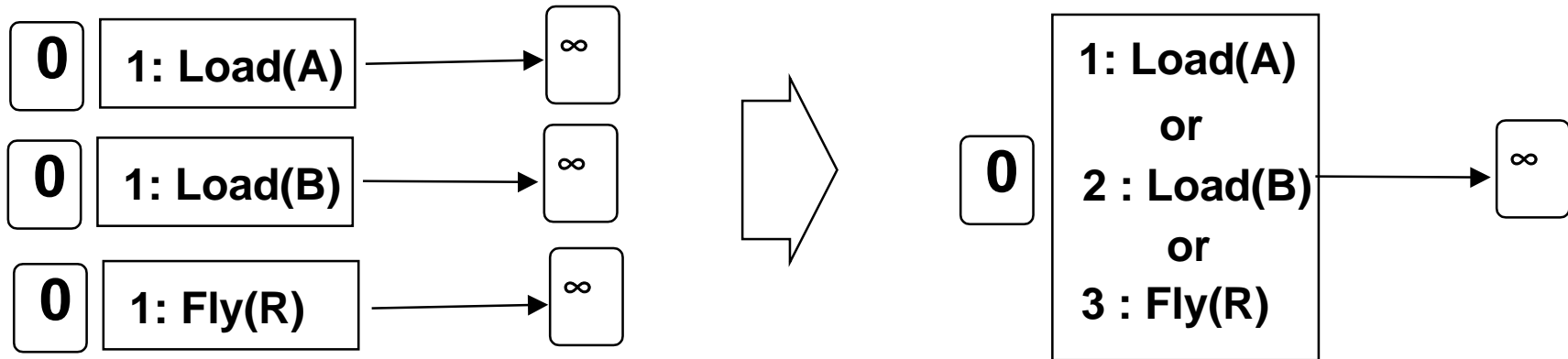
**EBL: Store interior node failure Explanations**



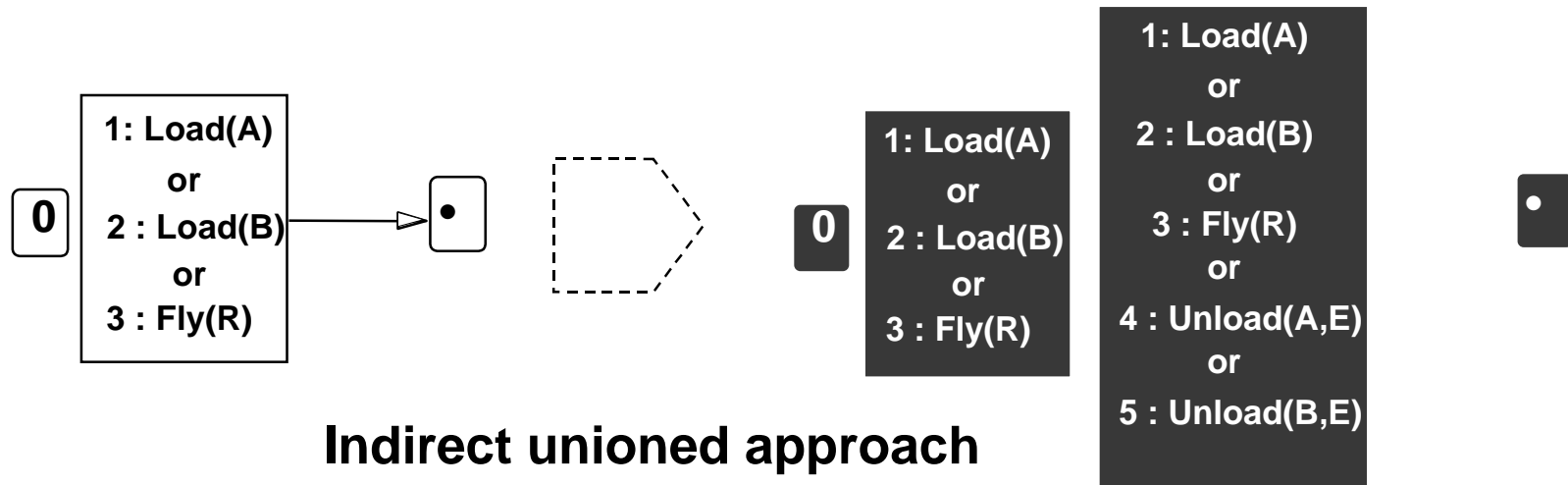
# Disjunctive Planning ..contd.

# Disjunctive Representations

--Allow disjunctive step, ordering and auxiliary constraints in partial plans

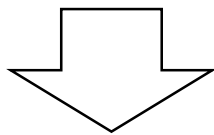


# Refining Disjunctive Plans (1)

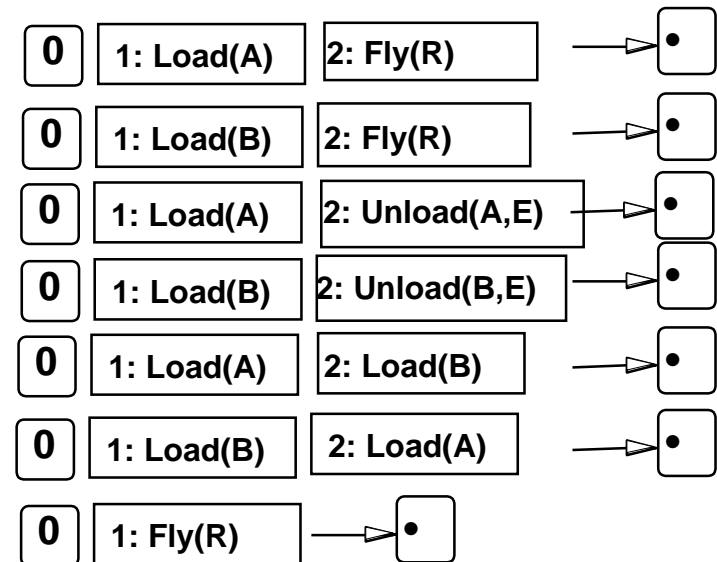
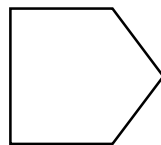
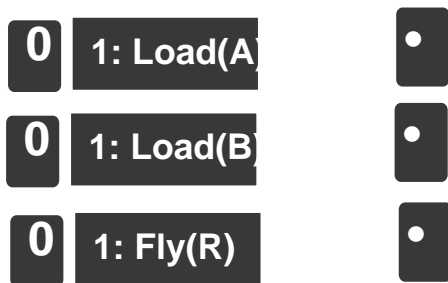


**Indirect unioned approach**

- + Maximum pruning power**
- Exponential refinement cost**



**INFEASIBLE**



# Refining Disjunctive plans (2)

Direct naive approach

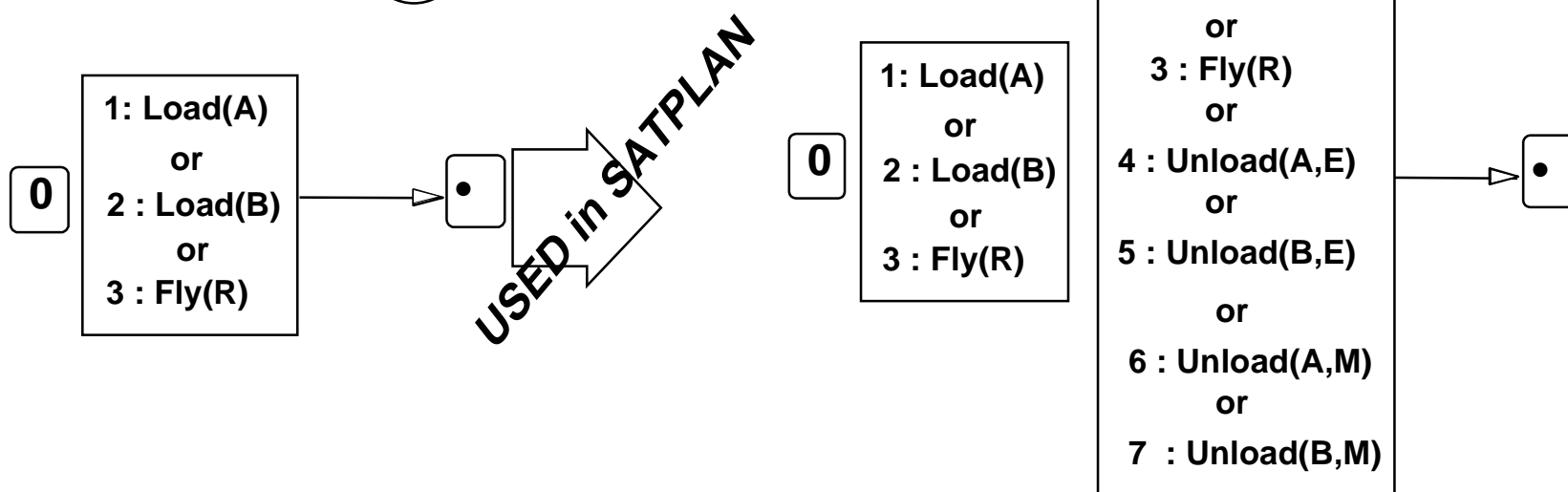
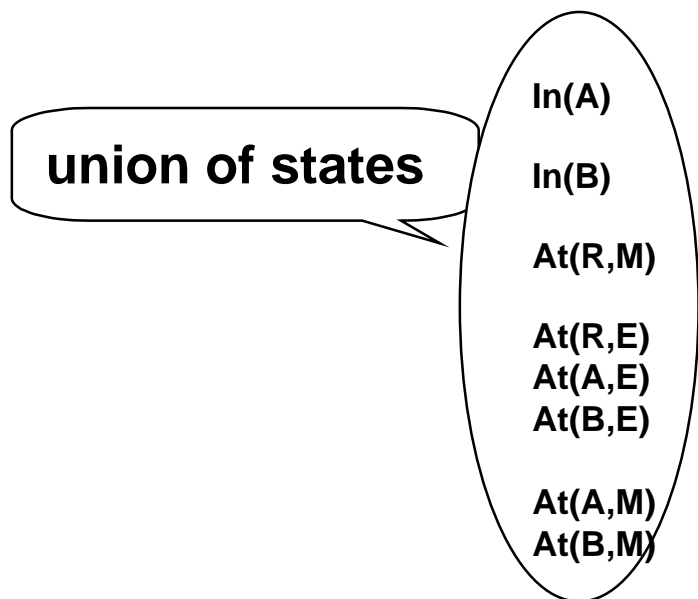
Put all actions at all levels

--Proposition list contains all conditions

+ Trivial to construct

- Loss of pruning power (progressivity)

=> Costlier solution extraction



# Refining Disjunctive plans (3)

Enforce partial 1-consistency

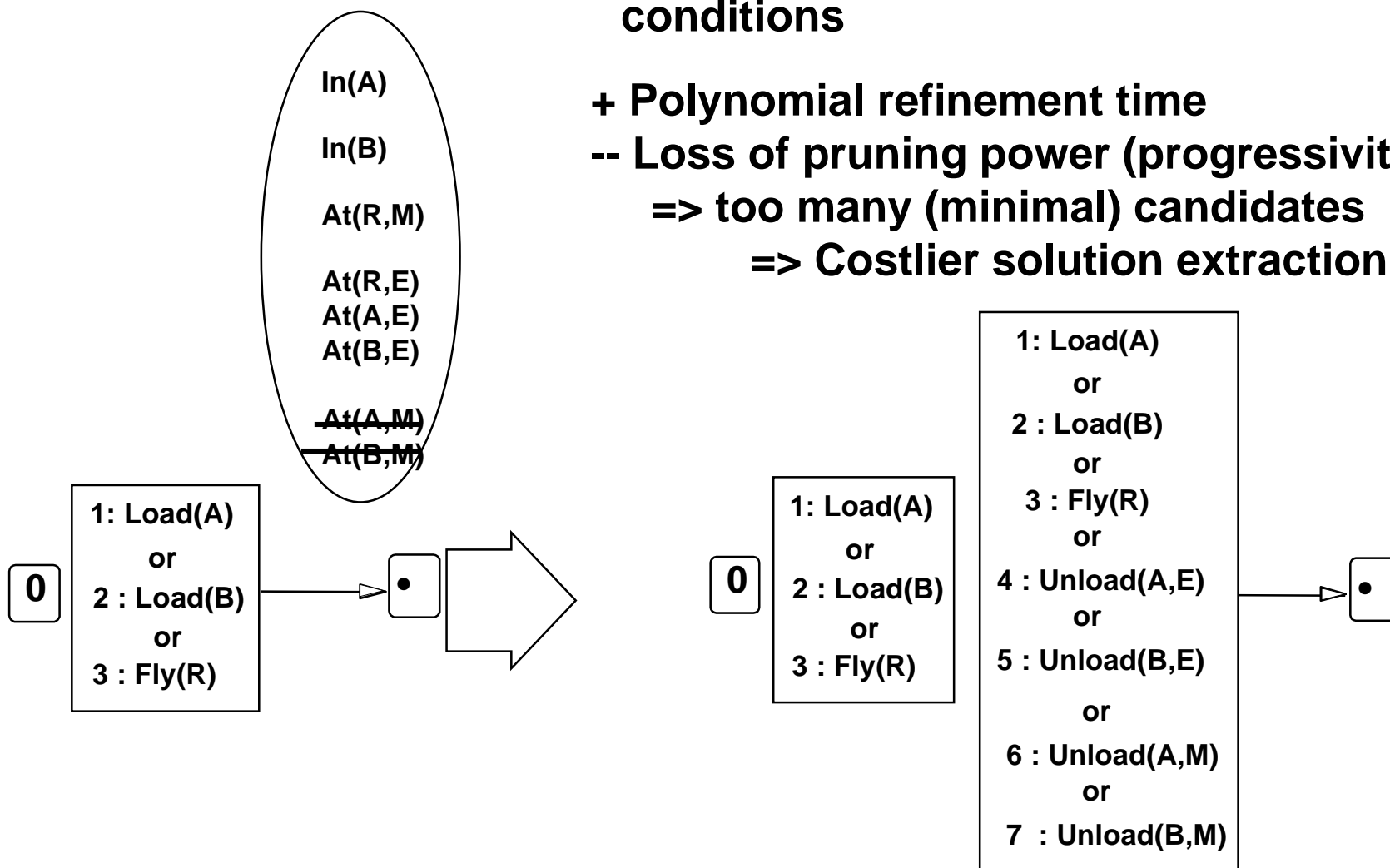
Proposition list avoids unsupported conditions

+ Polynomial refinement time

-- Loss of pruning power (progressivity)

=> too many (minimal) candidates

=> Costlier solution extraction



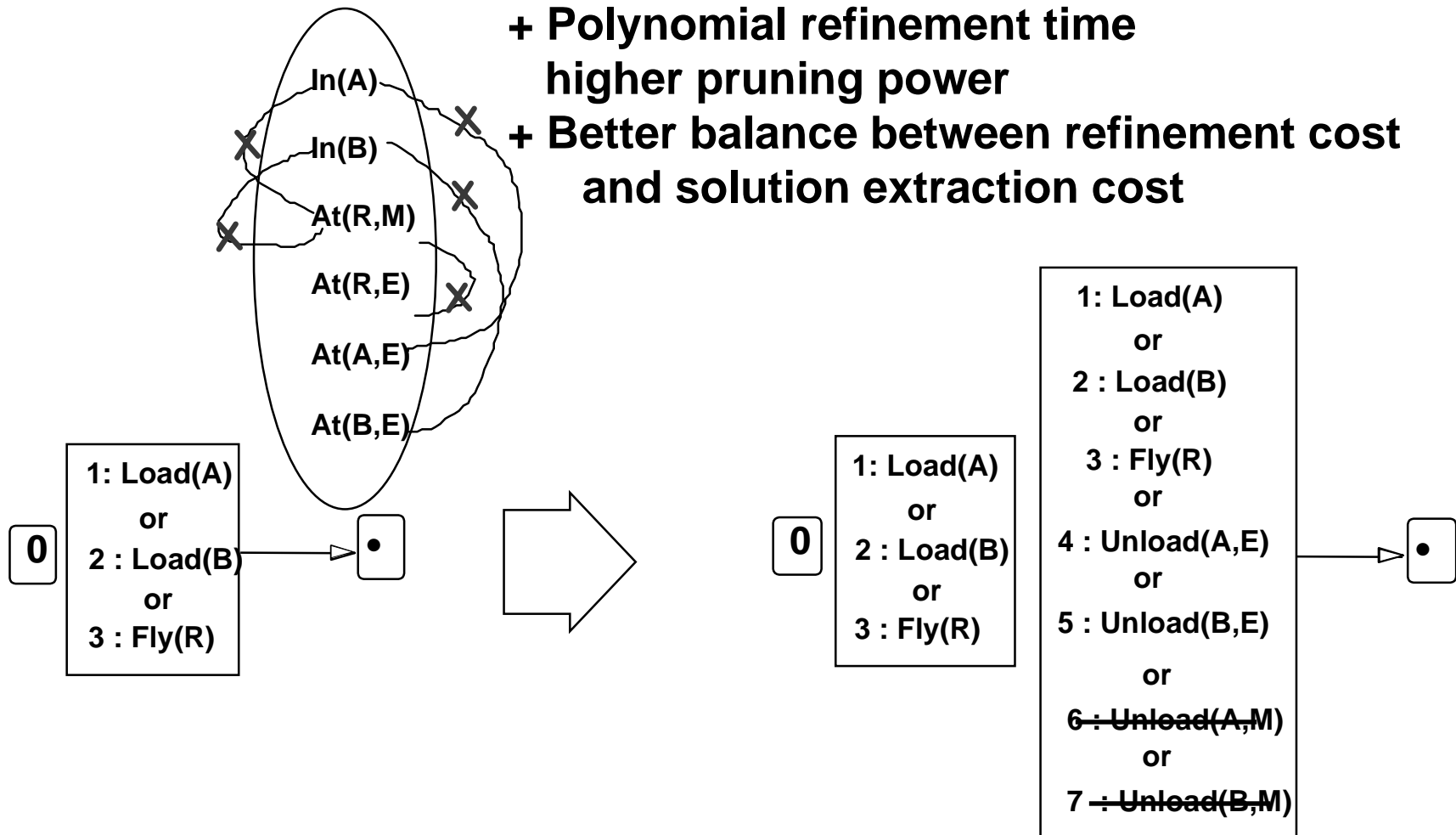
# Refining Disjunctive plans (4)

Enforce (partial) 2-consistency

Proposition list maintains interactions between pairs of conditions

+ Polynomial refinement time  
higher pruning power

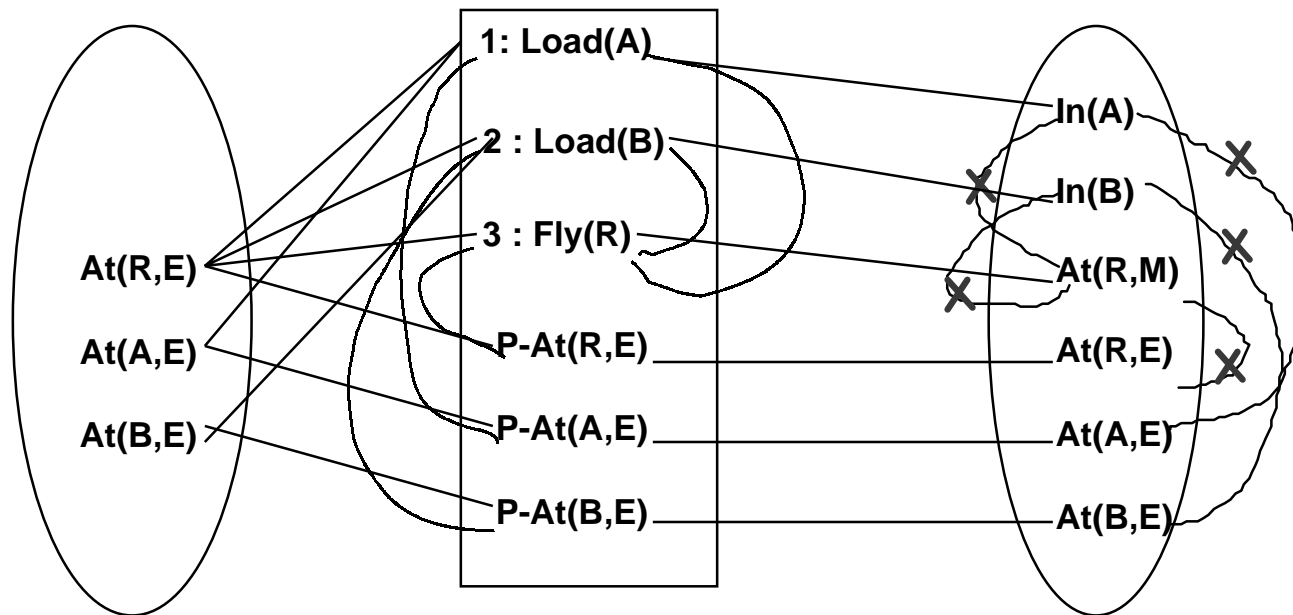
+ Better balance between refinement cost and solution extraction cost



# Graphplan Plangraph

(Blum & Furst, 1995)

- ◇ Graphplan directly refines disjunctive plans using forward state space refinement
  - The plan graph structure explicitly contains proposition lists, persistence actions for each condition, and dependency links between actions and propositions
  - Enforces partial 2-consistency by incrementally computing and propagating mutual exclusion relations



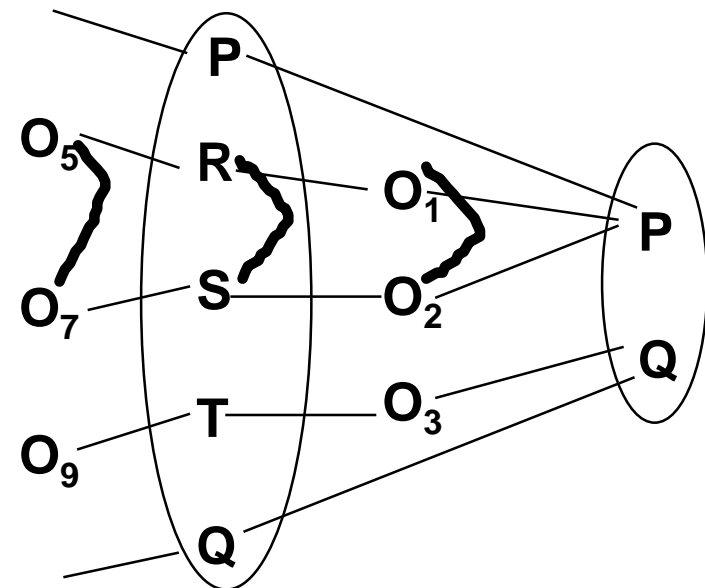


# Open issues in disjunctive refinement

- ✧ **Directed partial consistency**
  - **Mutex propagation is a form of reachability analysis**
    - » **Relevance analysis?**
  - **Higher levels of directional consistency?**
- ✧ **Supporting refinements other than FSR**
  - **Direct naïve refinements are easy to support; enforcing an appropriate level of consistency is harder**
  - **Some “relevance” based approaches exist for BSR**
    - » **Inseperability, backward mutex (see next)**
    - » **Can be used in conjunction with reachability analysis**
  - **Enforcing effective consistency for PSR is still virgin territory...**

# Ideas for enforcing consistency for BSR

- ✧ **1-consistency based on relevance**
  - Every action present in the final level will give either P or Q
- ✧ **Pairs of conditions or actions that will not be required together**
  - O1 or O2 is enough; so R or S is enough, so O5 or O7 is enough
- ✧ **Sets of conditions or actions that are “inseperable”**
  - P & Q are inseperable;
  - Set of actions supporting P is inseperable with that supporting Q



# Solution Extraction in Disjunctive Plans

- ✧ **Even after refinement, a k-length disjunctive plan contains too many potential k-length plans.**
- ✧ **Looking for a solution plan in the disjunctive structure is a combinatorial problem**
  - **Direct methods: Can be solved using special techniques customized to the disjunctive structure**
    - » **Graphplan backward search; Graphplan local search**
  - **Compilation: Can be polynomially compiled to any canonical combinatorial problems, including**
    - » **Constraint Satisfaction Problem (CSP)**
    - » **Boolean Satisfiability Problem (SAT)**
    - » **Integer Linear Programming (ILP)**

# Graphplan Backward Search

## (Direct Search I)

**Objective:** Find a sub-graph of the plangraph that corresponds to a valid plan.

**Method:** Start from the goal propositions at the last level

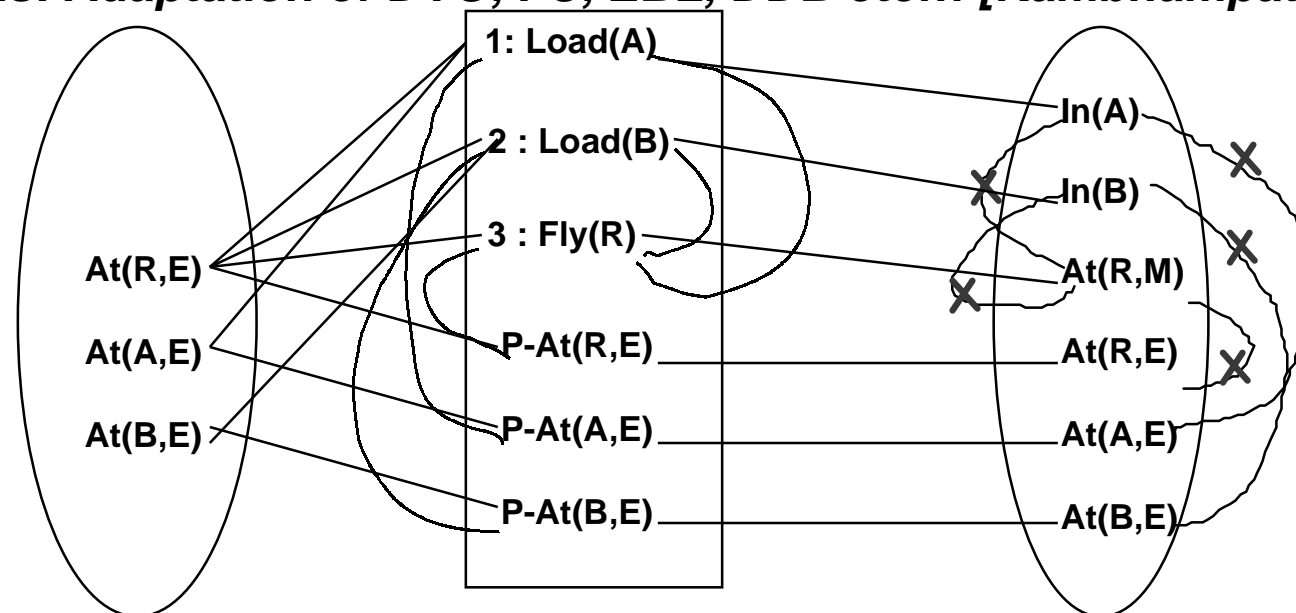
Select actions to support the goals so that no two are *mutex* (*choice*)

Recurse on the preconditions of the selected actions

(recursion ends at the initial state)

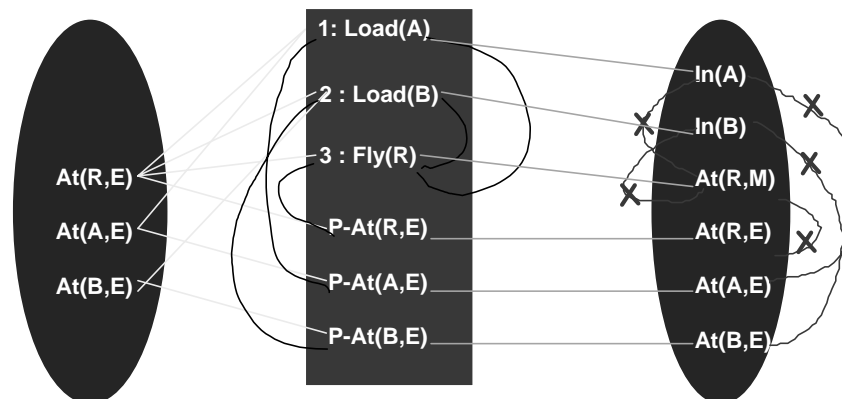
*(When backtracking over the goals at a level, memoize them)*

**Optimizations:** Adaptation of DVO, FC, EBL, DDB etc... [Kambhampati, IJCAI99]



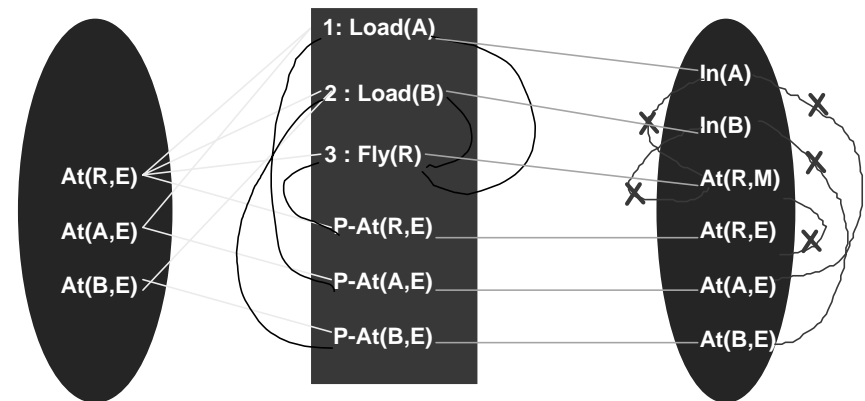
# Other Direct Extraction Strategies

- ✧ **Motivation: No compelling reason for making the search for a valid subgraph backward, or systematic...**
- ✧ **Alternatives:**
  - **Forward Search (dynamic programming) [Kambhampati & Parker 98; Blum & Langford 98]**
  - **Systematic Undirectional search [Rintanen, 98]**
    - » *Select an action anywhere in the plan-graph for inclusion in the solution; Propagate consequences (adapts normal CSP Search to plan-graph)*
  - **Local Search [Gerevini et. al., 99]**



# Compilation to CSP

Suppose we want to find a plan that satisfies  $In(A)$  &  $In(B)$



**Variables:** Propositions ( $In-A-1$ ,  $In-B-1$ , .. $At-R-E-0$  ...)

**Domains:** Actions supporting that proposition in the plan

$In-A-1 : \{ Load-A-1, \# \}$     $At-R-E-1: \{ P-At-R-E-1, \# \}$

**Constraints:** Mutual exclusion

$\sim [ ( In-A-1 = Load-A-1) \ \& \ ( At-R-M-1 = Fly-R-1) ] ; \text{ etc..}$

**Activation**

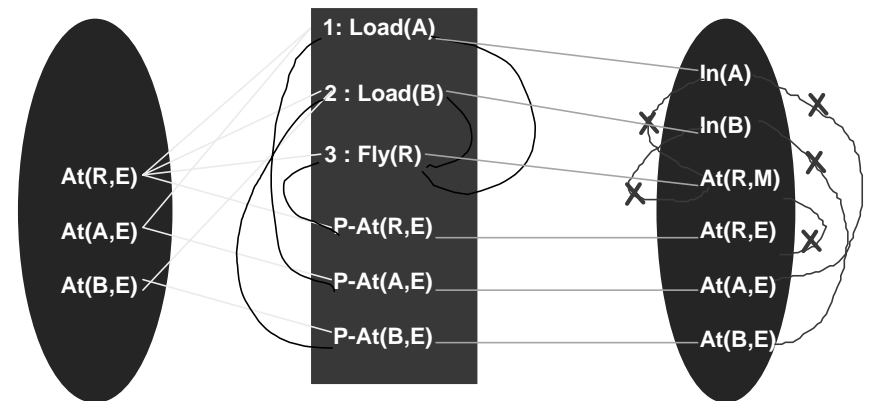
$In-A-1 \neq \#$     $In-B-1 \neq \#$    (Goals must have action assignments)

$In-A-1 = Load-A-1 \Rightarrow At-R-E-0 \neq \#$  ,  $At-A-E-0 \neq \#$

(subgoal activation constraints)

# Compilation to SAT

Suppose we want to find a plan that satisfies  $In(A)$  &  $In(B)$



Init:  $At-R-E-0$  &  $At-A-E-0$  &  $At-B-E-0$   
 Goal:  $In-A-1$  &  $In-B-1$

Graph: “*cond at  $k \Rightarrow$  one of the supporting actions at  $k-1$* ”

$In-A-1 \Rightarrow Load-A-1$     $In-B-1 \Rightarrow Load-B-1$   
 $At-R-M-1 \Rightarrow Fly-R-1$     $At-R-E-1 \Rightarrow P-At-R-E-1$

$Load-A-1 \Rightarrow At-R-E-0$  &  $At-A-E-0$       “*Actions  $\Rightarrow$  preconds*”  
 $Load-B-1 \Rightarrow At-R-E-0$  &  $At-B-E-0$   
 $P-At-R-E-1 \Rightarrow At-R-E-0$

$\sim In-A-1 \vee \sim At-R-M-1$     $\sim In-B-1 \vee \sim At-R-M-1$    “*Mutexes*”

# Compilation to Integer Linear Programming

## ✧ Motivations

- Ability to handle numeric quantities, and do optimization
- Heuristic value of the LP relaxation of ILP problems
- Deep connections between CSP and ILP (Chandru & Hooker, 99)

## ✧ Conversion

- Explicitly set up ILP inequalities corresponding to the disjunctive plan (Bylander, 97)
- Convert a SAT/CSP encoding to ILP inequalities
  - » E.g.  $X \vee \sim Y \vee Z \Rightarrow x + (1 - y) + z \geq 1$

## ✧ Solving

- Use LP relaxation as a heuristic (akin to Greedy Regression Graphs), or as a seed (for local search)
- Solve using standard methods (not competitive with SAT approaches)



# Direct generation of SAT encodings

- ✧ **Bounded-length plan finding can be posed directly as a SAT encoding (skipping the refinement step).**
  - **Set up k-length sequence of disjunctive actions ( $a_1 \vee a_2 \vee \dots \vee a_n$ )**
    - » **In effect, a direct naïve refinement is used (monotonic, complete, but not progressive)**
  - **Impose constraints, which when satisfied, will ensure that some sub-sequence of the disjunctive sequence is a solution to the planning problem**
    - » **The constraints set up lines of proof**

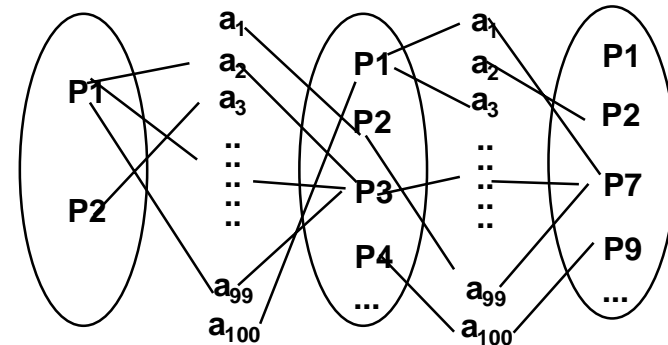
- **State-space proofs**

- **Causal proofs**

a1	a1	a1	a1
a2	a2	a2	a2
a3	a3	a3	a3
....	....	....	....
an	an	an	an
1	2		k

# Encodings based on state-based proofs

Propositions corresponding to initial conditions and goals are true at their respective levels  
 $P1-0 \ \& \ P2-0 \ \& \ P7-k \ \& \ P9-k$   
 At least one of the actions at each level will occur  
 $a1-j \ \vee \ a2-j \ \vee \ \dots \ \vee \ a_n-j$   
 Actions imply their preconditions and effects  
 $a_i-k \Rightarrow prec_{a_i-k-1} \ \& \ Eff_{a_i-k}$



## Progression (classical Frame)

A proposition P at j remains true if no action occurring at j+1 deletes P  
 $Pi-j \ \& \ Ak-(j+1) \Rightarrow Pi-j$   
 forall  $A_k$  that don't affect  $P_i$   
 No more than one action occurs at each step  
 $\sim aj-k \ \vee \ \sim am-k \ \text{forall } j,m,k$

## Regression (explanatory frame)

A proposition P changes values between j and j+1 only if an action occurs that makes it so  
 $\sim Pi-j \ \& \ Pi-(j+1) \Rightarrow a1-j \ \vee \ am-j ..$   
 Where  $a1, am, \dots$  add  $P_i$   
 No pair of interacting actions must occur together  
 $\sim aj-k \ \vee \ \sim am-k \ \text{forall } k$   
 forall  $aj, am$  that interfere

# Encodings based on Causal proofs

S0	S1	S2	S3	Sk	S $\infty$
	a1	a1	a1	a1	
Needs(S0, I1)	a2	a2	a2	a2	Needs(S $\infty$ , G1)
Needs(S0, I2)	a3	a3	a3	a3	Needs(S $\infty$ , G2)
□	....	....	....	....	
Needs(S0, In)	an	an	an	an	

Each step is mapped to exactly one action

$$Si = A1 \vee Si = A2 \dots ; \sim (Si = Ai \ \& \ Si = Aj)$$

A step inherits the needs, adds and deletes of the action it is mapped to

$$Si = Aj \Rightarrow \text{Adds}(Si, Pa) \ \& \ \text{Needs}(Si, Pp) \ \& \ \text{Deletes}(Si, Pd)$$

A Step get needs, adds and deletes only through mapped actions

$$\text{Adds}(Si, Pa) \Rightarrow Si = Aj \vee Si = Ak \dots \\ (Ai, Ak \ \text{add} \ Pa)$$

Every need is established by some step

$$\text{Needs}(Si, Pj) \Rightarrow \text{Estab}(S1, Pj, Si) \vee \\ \text{Estab}(S2, Pj, Si) \dots \vee \text{Estab}(Sk, Pj, Si)$$

Establishment with causal links

$$\text{Estab}(S1, Pj, Si) \Rightarrow \text{Link}(S1, Pj, Si)$$

Link implies addition & precedence

$$\text{Link}(Si, Pj, Sk) \Rightarrow \text{Adds}(Si, Pj) \ \& \ \text{Precedes}(Si, Pj)$$

Link implies preservation by intervening steps

$$\text{Link}(Si, Pj, Sk) \ \& \ \text{Deletes}(Sm, Pj) \\ \Rightarrow \text{Precedes}(Sm, Si) \vee \\ \text{Precedes}(Sk, Si)$$

Precedence is irreflexive, asymmetric and transitive...

# Alternative causal encodings

<b>S0</b>	<b>S1</b>	<b>S2</b>	<b>S3</b>	<b>Sk</b>	<b>S∞</b>
	a1	a1	a1	a1	
Needs(S0, I1)	a2	a2	a2	a2	Needs(S∞, G1)
Needs(S0, I2)	a3	a3	a3	a3	Needs(S∞, G2)
□	....	....	....	....	
Needs(S0, In)	an	an	an	an	

## Whiteknight based establishment

Some preceding step adds

$Estab(S1, Pj, Si) \Rightarrow Adds(S1, Pj)$   
 &  $Precedes(S1, Sj)$

For every preceding step deleting a needed condition, there is a white-knight that adds it back

$Needs(Sj, Pj) \& Deletes(Sd, Pj) \& Precedes(Sd, Sj)$   
 $\Rightarrow Wknight(S1, Sj, Sd, Pj) \vee$   
 $Wknight(S2, Sj, Sd, Pj) \vee \dots$

$Wknight(Sw, Sj, Sd, Pj) \Rightarrow Precedes(Sw, Sj) \&$   
 $Precedes(Sd, Sw) \& Adds(Sw, Pj)$

**Eliminates the need for  $O(k^2)$  causal link variables**

## Contiguity based precedence

Step  $Sj$  is in position  $j$

$Precedes(S1, S2)$   
 $Precedes(S1, S3)$

.....  
 $Precedes(Sj, Sj+k)$

**Eliminates the need for  $O(k^3)$  Transitivity clauses**

# Simplifying SAT encodings

- ✧ **Constraint propagation...**
  - Unit propagation  $P, \sim P \vee Q \Rightarrow Q$
  - Pure literal elimination (If a proposition occurs with the same polarity in any clause that it occurs in, set it to True)
    - » Works only when all satisfying assignments are considered equivalent [Wolfe & Weld, IJCAI-99]
- ✧ **Syntactic manipulations:**
  - Resolve away dependent variables
    - » Fluent or Action variables can be eliminated in state-based encodings
      - $P11 \rightarrow A12 \rightarrow P22$  becomes  $P11 \Rightarrow P22$
- ✧ **Compilation Tricks**
  - Split n-ary actions & propositions to 2-ary ones
    - »  $\text{Move}(x,y,z,t)$  leads to  $O(\#obj * \#obj * \#obj * k)$  variables
    - »  $\text{MB}(x,t), \text{MF}(y,t), \text{M}(z,t)$  leads to  $3 * O(\#obj, k)$  variables
  - Lifting (variablized encodings)???

# Tradeoffs between encodings based on different proof strategies

- ✧ Progression (classical frame) encodings lead to higher number of clauses, and allow only serial plans
  - $O(\text{\#prop} * \text{\#actions} * \text{\#levels})$
  - To allow parallel plans, we need to look at frame axioms with sets of actions, increasing the clauses exponentially
- ✧ Regression (explanatory frame) encodings reduce clauses, and allow parallel plans
  - $O(\text{\#prop} * \text{\#levels})$
- ✧ Empirical results validate dominance of regression over progression encodings
  - The SAT compilation of Graphplan plan-graph corresponds to a form of backward encoding

## Tradeoffs between encodings based on different proof strategies

- ✧ **Causal encodings in general have more clauses than state-space encodings**
  - **$O(\#actions \times \#actions \times \#fluents)$  for causal link variables**
    - » **Could be reduced by using white-knight based proofs**
  - **$O(\#actions \times \#actions \times \#actions)$  clauses for partial ordering**
    - » **Could be reduced by using contiguous ordering**
  - **However, the best causal encodings will still be dominated by the backward state-space encodings [Mali & Kambhampati, 99]**
- ✧ **Paradoxical given the success of partial order planners in conjunctive planning?**
  - **Not really! We are using causal proof which is typically longer than state-based proofs, and are not using the flexibility of step insertion.**
    - » **Can be helpful in incremental planning & Plan reuse**
    - » **Are helpful in using causal domain specific knowledge (e.g. HTN schemas)**

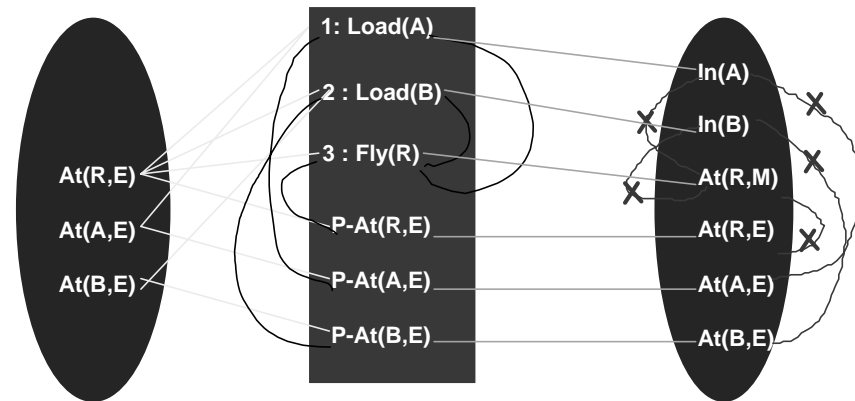
# Direct compilation vs. compilation of refined disjunctive plans

- ✧ **Direct encodings correspond to translation of Direct Naïve refinements**
  - **Non-progressive, have large number of minimal candidates compared to encodings based on refined disjunctive plans (such as Graphplan plan-graph)**
  - **Enforcing consistency at SAT level is costly (lack of direction)**
- ✧ **And yet, SATPLAN, that used direct SAT encodings did better than Graphplan, that worked with plangraph...**
  - **Paradox? NOT.. It just shows that the solution extraction through SAT was better than through vanilla Graphplan backward search! [Kambhampati, IJCAI-97; Rintanen, KR-98]**
    - » **Blackbox [IJCAI-99] uses encodings based on planning graph**



# On the difficulty of enforcing directional consistency at the SAT level

- ✧ Partial consistency that is enforced by refinement of disjunctive plans can also be done at the SAT level through resolution
  - But the resolution will be undirected
    - » will consider clauses from multiple levels
  - and thus can be costly
- ✧ Moral: Refinements allow *directed* consistency enforcement..



~ load-A-1  $\vee$  ~load-B-1]  
 in-A-1  $\Rightarrow$  load-A-1  
 in-B-1  $\Rightarrow$  load-B-1

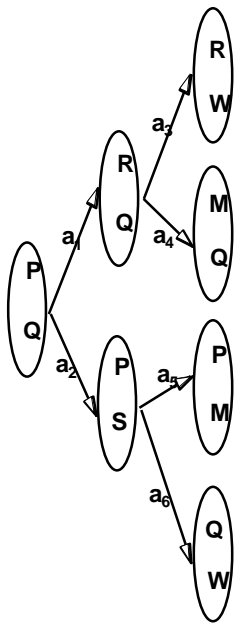
With resolution, we get  
 ~In-A-1  $\vee$  ~In-A-2

# Impact of Refinements on Encoding Size

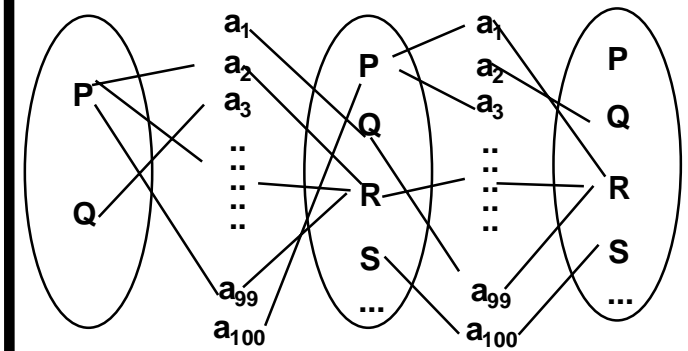
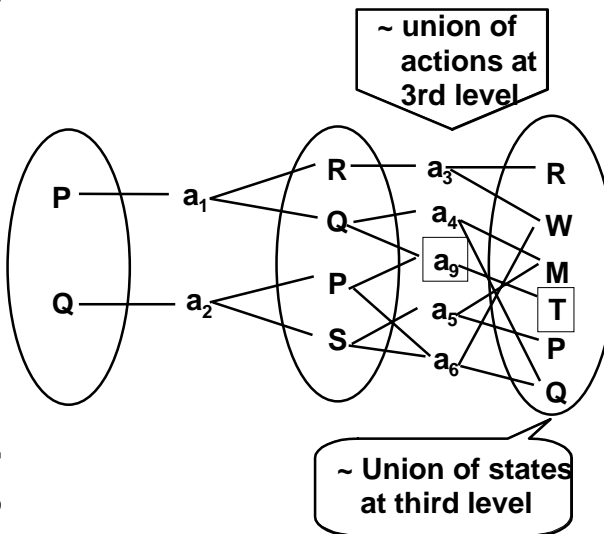
Encodings based on “refined” plans

Direct SAT Encoding

Refined plan sets



Disj. plans + Constraint Prop.



Encoding size increases & Cost of generating encoding reduces

- Encodings based on refined plans can be more compact
- *Smaller clauses, fewer variables ...*

## Direct vs. compiled solution extraction

### DIRECT

- x Need to adapt CSP/SAT techniques**
- ✓ Can exploit approaches for compacting the plan**
- ✓ Can make the search incremental across iterations**

### Compiled

- ✓ Can exploit the latest advances in SAT/CSP solvers**
- x Compilation stage can be time consuming, leads to memory blow-up**
- x Makes it harder to exploit search from previous iterations**
- ✓ Makes it easier to add declarative control knowledge**

## Some implemented disjunctive planners

	Refinement	Solution Extraction
<b>Graphplan</b> (Blum & Furst) <ul style="list-style-type: none"> <li>-- IPP                              (Koehler et. al.)</li> <li>-- STAN                              (Fox et. al.)</li> <li>--GP-EBL                              (Kambhampati)</li> </ul>	<i>Partially</i> <i>2-consistent direct</i> <i>refinement</i> using FSR	Direct search on the disjunctive plan (+ adaptation of CSP techniques such as DDB, EBL, DVO, FC etc)
<b>SATPLAN</b> (Kautz & Selman)	<i>Naïve direct</i> <i>refinement</i> with FSR, BSR, PSR	Compilation to SAT
<b>Blackbox</b> (Kautz & Selman)	<i>Same as Graphplan</i>	Compilation to SAT

# Accelerating Disjunctive Planners

- ✧ **Reduce the size of the disjunctive plan**
  - Relevance based pruning
    - » Backward plan growth [Kambhampati et. al., 97]
    - » Preprocessing to remove irrelevant actions and conditions [RIFO, Nebel et. al. 97]
- ✧ **Increase the consistency level of the disjunctive plan**
  - Learn (or input) higher-order mutexes (invariants) [Gerevini, 98]
- ✧ **Improve the solution extraction process**
  - Exploit Symmetry [Fox et. al. 99, Srivastava et. al. 99]

# Conjunctive vs. Disjunctive planners

- ✧ Progress depends on the effectiveness of the heuristics for judging the goodness of a partial plan
- ✧ Search control may be easier to articulate
- ✧ Space consumption can be regulated
- ✧ Better fit with mixed-initiative, incremental planning scenarios(?)
- ✧ Space consumption is a big issue
  - Creation and storage of disjunctive structures
    - » The AT&T benchmark experiments were done on a 8-gig RAM m/c!
    - » E.g. TLPlan beats disjunctive planners at 800-block problems...
- ✧ Better integration with non-propositional reasoners (?)

Hybrid planners--Controlled splitting &  
Search in the space of disjunctive plans

# Controlled Splitting

## Refine ( $\underline{P}$ : Plan)

- 0\*. If  $\underline{P}$  is inconsistent, prune it. End.
1. If a minimal candidate corresponds to a solution, terminate.
2. Apply a refinement strategy  $\underline{R}$  to  $\underline{P}$  to get a new plan set  $\underline{P}'$
3. Reduce components of  $\underline{P}'$  by introducing disjunction
4. Propagate constraints in the components
5. Non-deterministically select a component  $\underline{P}'_i$  of  $\underline{P}'$   
Call Refine( $\underline{P}'_i$ )

DESCARTES [Joslin & Pollack; 1995]  
UCPOP-D [Kambhampati & Yang; KR, 1996]  
Just scratch the surface...

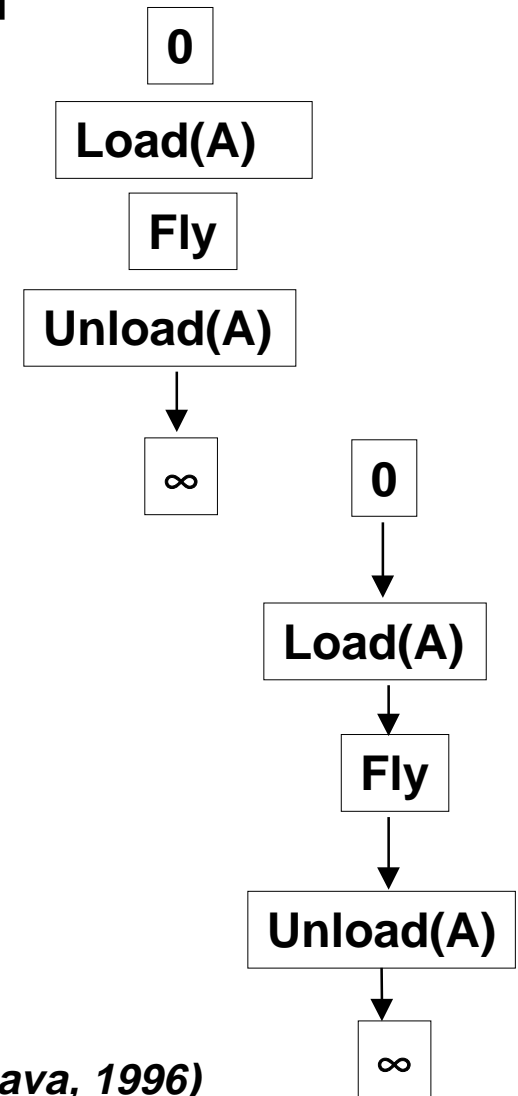
# Characterizing Difficult Problem Classes

- ✧ **There is a nice theory of Serializability for conjunctive planning**
- ✧ **There is no clean theory yet of what makes a problem easy or hard for disjunctive planners**
  - **Hardness characterizations in CSP/SAT can be used.**



# Subgoal Interactions and Planner Selection

- ✧ Every refinement planner R can be associated with a class  $C_R$  of partial plans
- ✧  $G_1$  and  $G_2$  are trivially serializable w.r.t. a plan class C if every subplan  $P_{G_i} \in C$  is extendable to a plan for solving both.
  - commitment  $\downarrow \Rightarrow$  trivial serializability  $\uparrow$
  - commitment  $\downarrow \Rightarrow$  plan handling cost  $\uparrow$
- $\Rightarrow$  Select the planner producing the class of highest commitment plans w.r.t. which most problems are trivially serializable



*(Korf, 1987; Barrett & Weld, 1994; Kambhampati, Ihrig and Srivastava, 1996)*

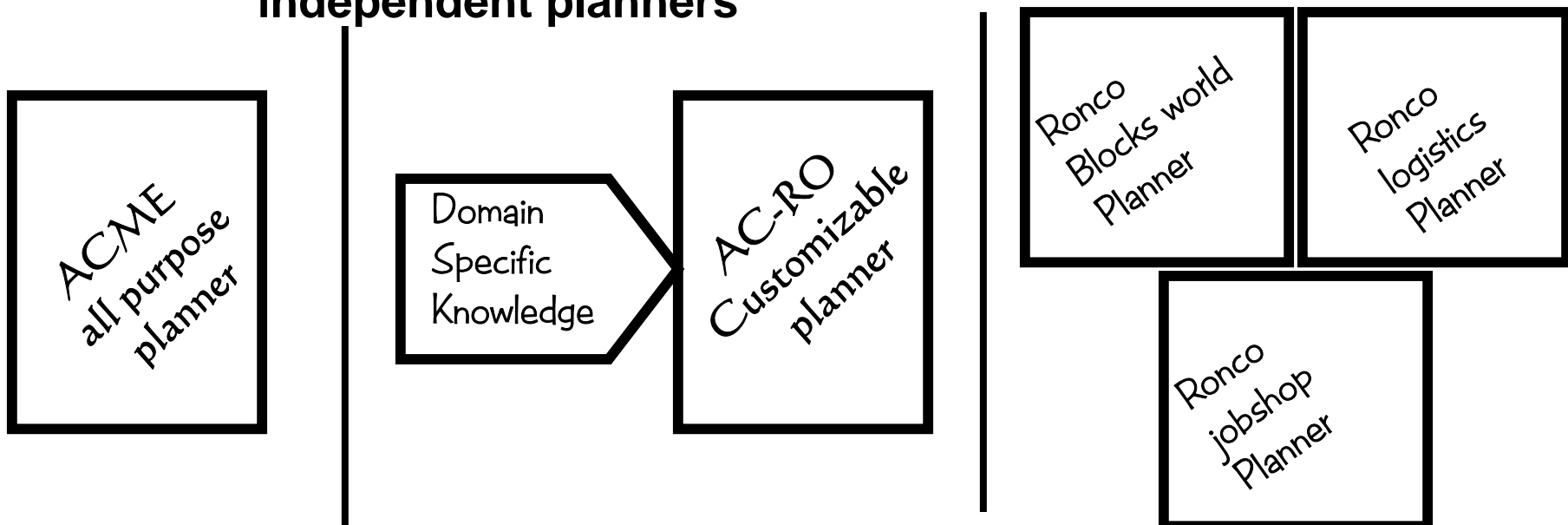
# CUSTOMIZING PLANNERS WITH DOMAIN SPECIFIC KNOWLEDGE

- 1. User-assisted customization**  
(accept domain-specific knowledge as input)
- 2. Automated customization**  
(learn regularities of the domain through experience)

# User-Assisted Customization (using domain-specific Knowledge)

- ✧ Domain independent planners tend to miss the regularities in the domain
- ✧ Domain specific planners have to be built from scratch for every domain

An “*Any-Expertise*” Solution: Try adding domain specific control knowledge to the domain-independent planners



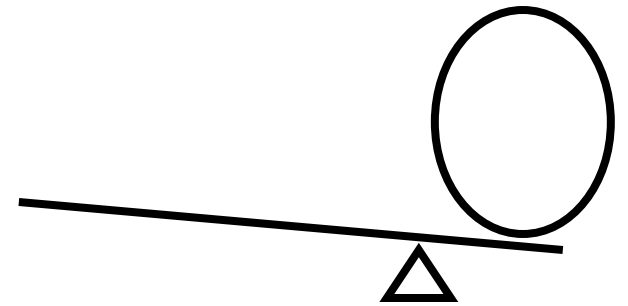
# Many User-Customizable Planners

- ✧ **Conjunctive planners**
  - HTN planners
    - » SIPE [Wilkins, 85-]
    - » NONLIN/O-Plan [Tate et. al., 77-]
    - » NOAH [Sacerdoti, 75]
    - » Also SHOP (Nau et. al., IJCAI-99)
  - State-space planners
    - » TLPlan [Bacchus & Kabanza, 95]
  - Customization frameworks
    - » CLAY [Srivastava & Kambhampati, 97]
  - Planning & Learning
    - » Prodigy+EBL , UCPOP+EBL, DerSNLP+EBL ..
- ✧ **Disjunctive planners**
  - HTN SAT [Mali & Kambhampati, 98]
  - SATPLAN+Dom [Kautz & Selman, 98]

How do they relate?  
What are the tradeoffs?

# With enough domain knowledge any level of performance can be achieved...

- ✧ HTN-SAT, SATPLAN+DOM beat SATPLAN...
  - Expect reduction schemas, declarative knowledge about inoptimal plans
- ✧ TLPLAN beats SATPLAN, GRAPHPLAN
  - But uses quite detailed domain knowledge
- ✧ SHOP beats TLPLAN...
  - Expects user to write a “program” for the domain in its language
    - » Explicit instructions on the order in which schemas are considered and concatenated



*Who gets the credit?  
-The provider of domain knowledge?  
-The planner that is capable of using it?*

# Types of domain-specific knowledge

- ✧ **Declarative knowledge about desirable or undesirable solutions and partial solutions (SATPLAN+DOM)**
- ✧ **Declarative knowledge about desirable/undesirable search paths (TLPlan)**
- ✧ **A declarative grammar of desirable solutions (HTN)**
- ✧ **Procedural knowledge about how the search for the solution should be organized (SHOP)**

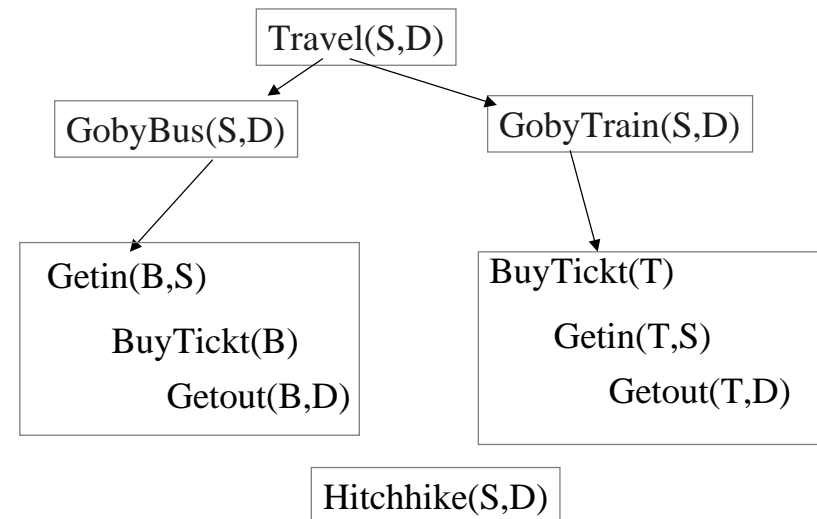
# Uses of Domain-specific knowledge

- ✧ **As declarative search control**
  - HTN schemas, TLPlan rules
- ✧ **As procedural guidance**
  - (SHOP)
- ✧ **As declarative axioms that are used along with other knowledge**
  - SATPlan+Domain specific knowledge
- ✧ **Folded into the domain-independent algorithm to generate a new domain-customized planner**
  - CLAY

# Task Decomposition (HTN) Planning

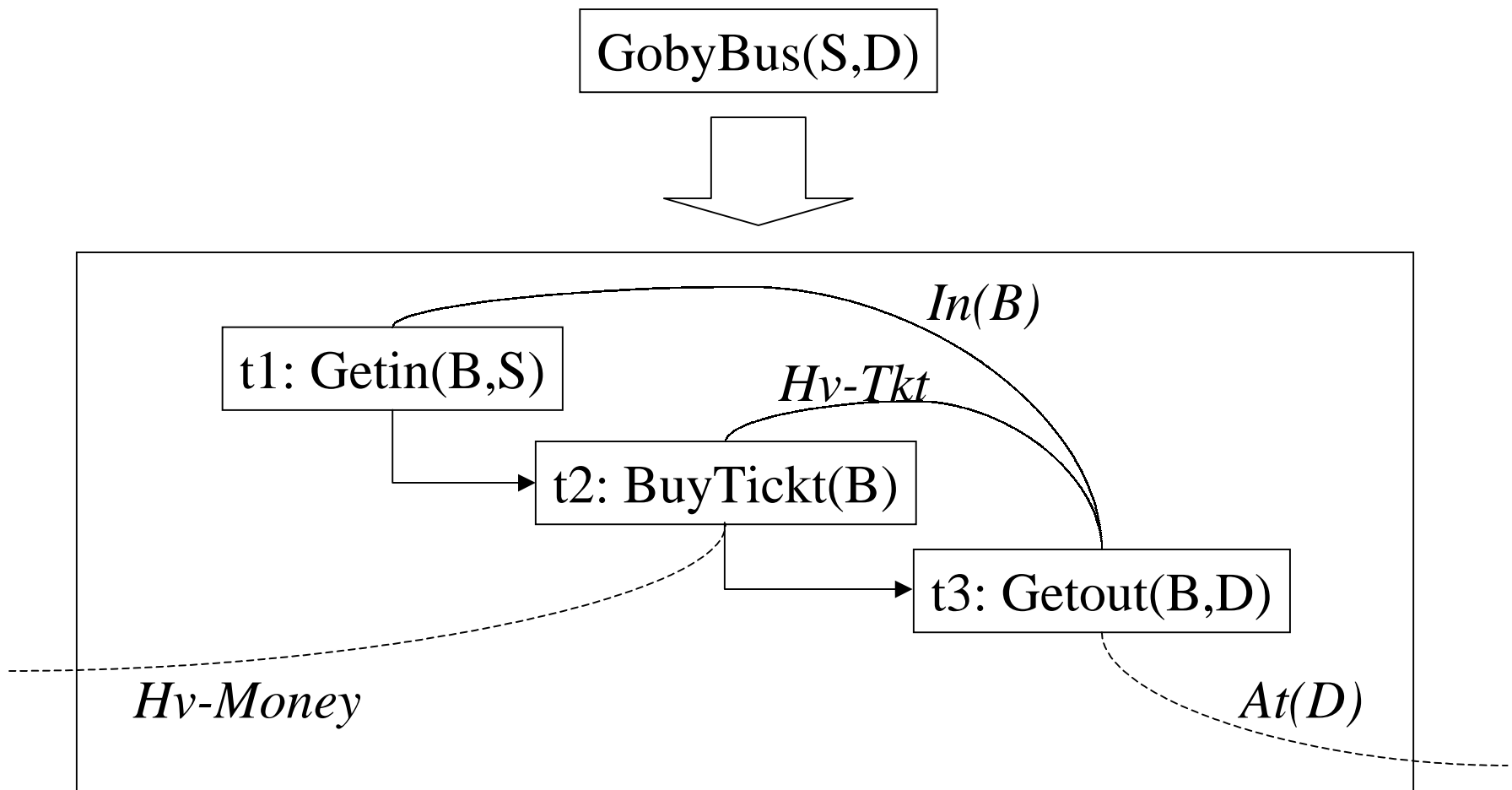
- ✧ The OLDEST approach for providing domain-specific knowledge
  - Most of the fielded applications use HTN planning
- ✧ Domain model contains non-primitive actions, and schemas for reducing them
- ✧ Reduction schemas are given by the designer
  - Can be seen as encoding user-intent
    - » *Popularity of HTN approaches a testament of ease with which these schemas are available?*

- ✧ Two notions of completeness:
  - Schema completeness
    - » (Partial Hierarchicalization)
  - Planner completeness

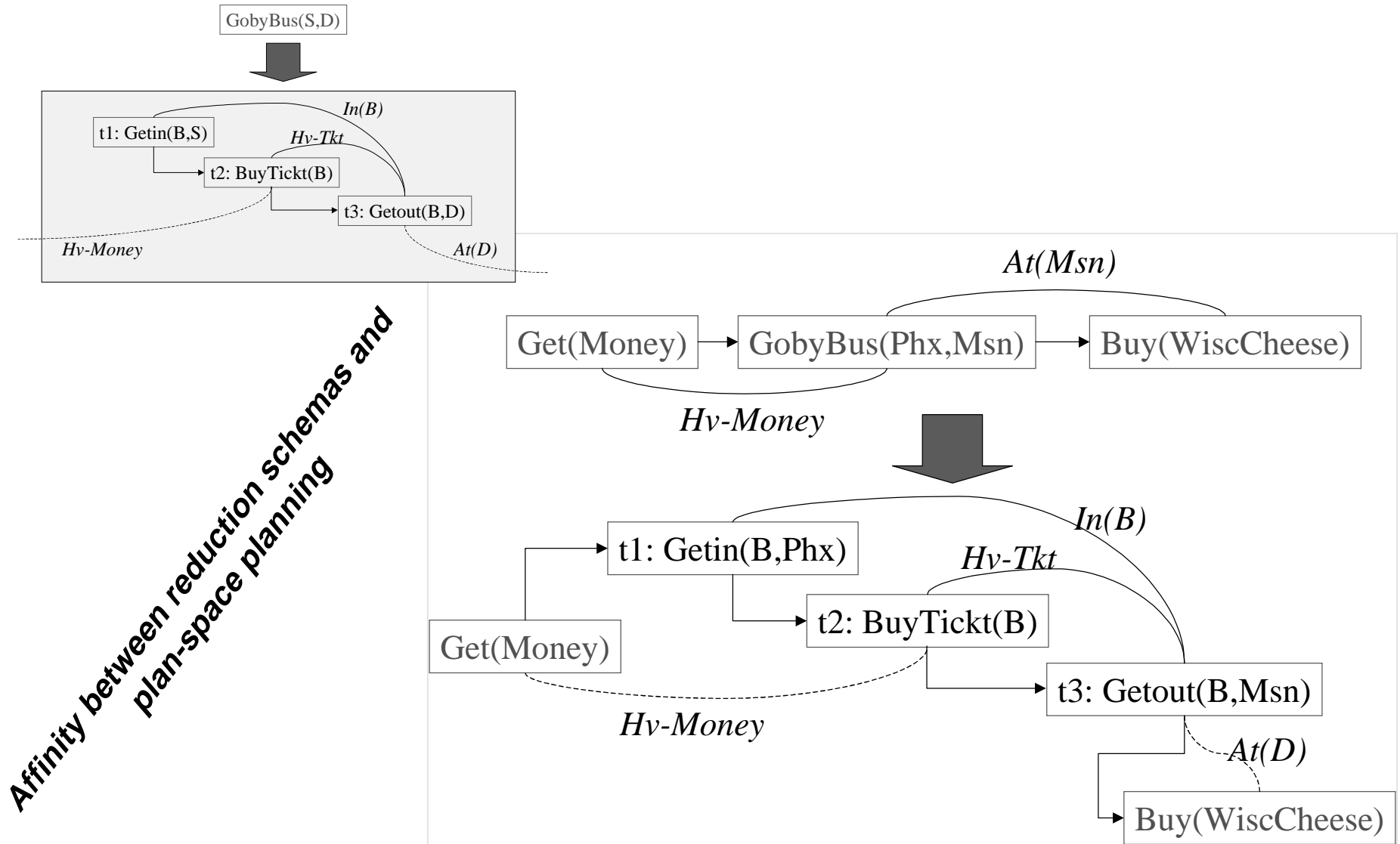




# Modeling Reduction Schemas



# Modeling Action Reduction



# Dual views of HTN planning

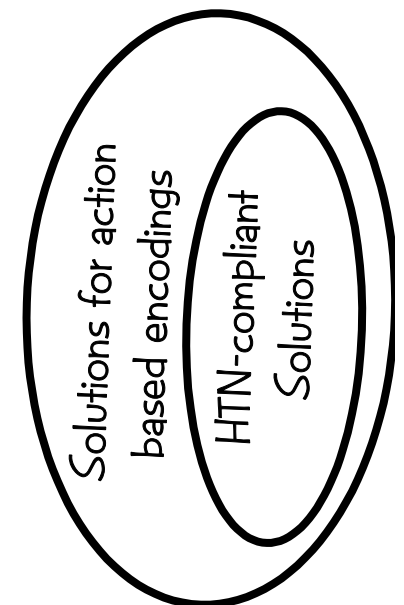
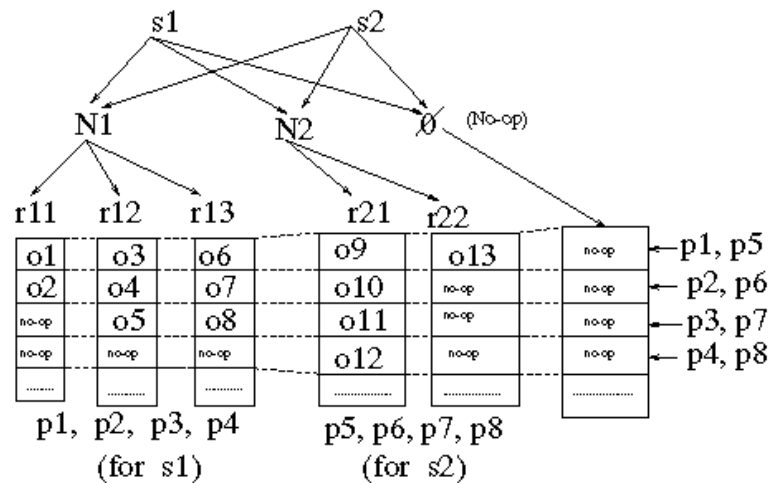
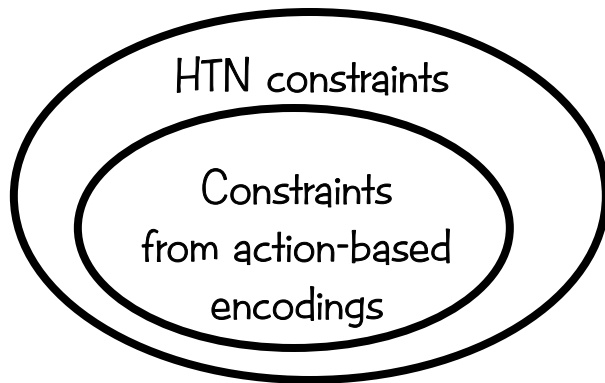
- ◇ **Capturing hierarchical structure of the domain**
    - **Motivates top-down planning**
      - » **Start with abstract plans, and reduce them**
  - ◇ **Many technical headaches**
    - **Respecting user-intent, maintaining systematicity and minimality**
      - [Kambhampati et. al. AAAI-98]
      - » **Phantomization, filters, promiscuity, downward-unlinearizability..**
- ◇ **Capturing expert advice about desirable solutions**
    - **Motivates bottom-up planning**
      - » **Ensure that each partial plan being considered is “legal” with respect to the reduction schemas**
      - » **Directly usable with disjunctive planning approaches**
  - ◇ **Connection to efficiency is not obvious**

*Relative advantages are still unclear...*

*[Barrett, 97]*

# SAT encodings of HTN planning

- ◇ Abstract actions can be seen as disjunctive constraints
  - K-step encoding has each of the steps mapped to a disjunction of the non-primitive tasks
  - If a step  $s$  is mapped to a task  $N$ , then one of the reductions of  $N$  must hold (\*\*The heart of encoding setup\*\*)
  - + The normal constraints of primitive action-based encoding
    - » Causal encodings seem to be a natural fit (given the causal dependencies encoded in reduction schemas)



# Solving HTN Encodings

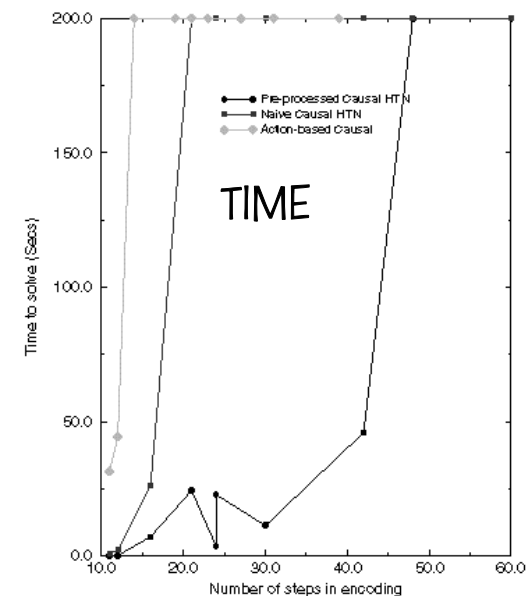
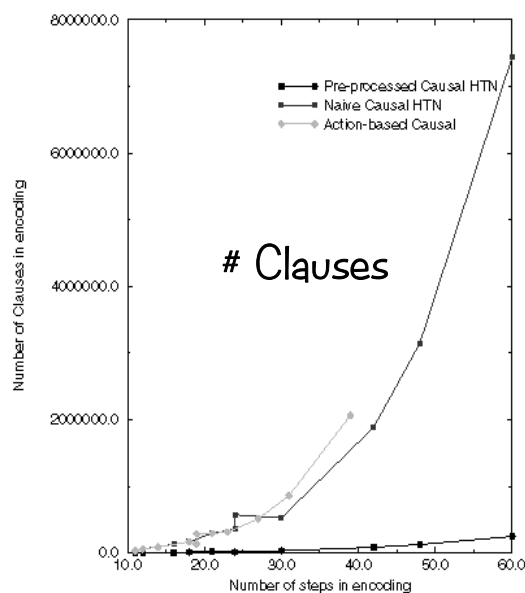
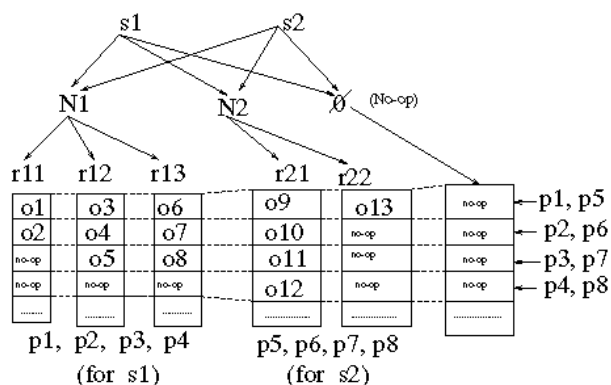
**Puzzle: How can increasing encoding sizes lead to efficient planning?**

**Abstract actions and their reductions put restrictions on the amount of step-action disjunction at the primitive level.**

**--Reduction in step-action disjunction propagates**

**e.g. Fewer causal-link variables, Fewer exclusion clauses...**

**Savings won't hold if each non-primitive task has MANY reductions**



# Non-HTN domain knowledge for SAT encodings

Invariants: *A truck is at only one location*

$$at(truck, loc1, I) \ \& \ loc1 \neq loc2 \Rightarrow \sim at(truck, loc2, I)$$

Optimality: *Do not return a package to a location*

$$at(pkg, loc, I) \ \& \ \sim at(pkg, loc, I+1) \ \& \ I < J \Rightarrow \sim at(pkg, loc, j)$$

Simplifying: *Once a truck is loaded, it should immediately move*

$$\sim in(pkg, truck, I) \ \& \ in(pkg, truck, I+1) \ \& \ at(truck, loc, I+1) \Rightarrow \\ \sim at(truck, loc, I+2)$$

**Once again, additional clauses first increase the encoding size  
but make them easier to solve after simplification  
(unit-propagation etc).**

# Rules on desirable State Sequences: TLPlan approach

TLPlan [Bacchus & Kabanza, 95/98] controls a forward state-space planner

Rules are written on state sequences using the linear temporal logic (LTL)

LTL is an extension of prop logic with temporal modalities

U	until	[]	always
O	next	<>	eventually

Example:

If you achieve  $\text{on}(B,A)$ , then preserve it until  $\text{On}(C,B)$  is achieved:

$[] ( \text{on}(B,A) \Rightarrow \text{on}(B,A) \text{ U } \text{on}(C,B) )$

# TLPLAN Rules can get quite boroque

Good towers are those that do not violate any goal conditions

$$\begin{aligned} \text{goodtower}(x) &\triangleq \text{clear}(x) \wedge \text{goodtowerbelow}(x) \\ \text{goodtowerbelow}(x) &\triangleq (\text{ontable}(x) \wedge \neg \text{GOAL}(\exists [y:\text{on}(x, y)] \vee \text{holding}(x))) \\ &\vee \exists [y:\text{on}(x, y)] \neg \text{GOAL}(\text{ontable}(x) \vee \text{holding}(x)) \wedge \neg \text{GOAL}(\text{clear}(y)) \\ &\wedge \forall [z:\text{GOAL}(\text{on}(x, z))] z = y \wedge \forall [z:\text{GOAL}(\text{on}(z, y))] z = x \\ &\wedge \text{goodtowerbelow}(y) \end{aligned}$$

Keep growing “good” towers, and avoid “bad” towers

$$\begin{aligned} \square & \left( \forall [x:\text{clear}(x)] \text{goodtower}(x) \Rightarrow \bigcirc \text{goodtowerabove}(x) \right. \\ & \wedge \text{badtower}(x) \Rightarrow \bigcirc (\neg \exists [y:\text{on}(y, x)]) \\ & \wedge (\text{ontable}(x) \wedge \exists [y:\text{GOAL}(\text{on}(x, y))] \neg \text{goodtower}(y)) \\ & \left. \Rightarrow \bigcirc (\neg \text{holding}(x)) \right) \end{aligned}$$

How “Obvious”  
are these rules?

**The heart of TLPlan is the ability to *incrementally* and *effectively* evaluate the truth of LTL formulas.**



# Full procedural control: The SHOP way

Shop provides a “high-level” programming language in which the user can code his/her domain specific planner

- Similarities to HTN planning
- Not declarative (?)

The SHOP engine can be seen as an interpreter for this language

```
(:method (travel-to ?y)
  (:first (at ?x)
    (at-taxi-stand ?t ?x)
    (distance ?x ?y ?d)
    (have-taxi-fare ?d))
  `((!hail ?t ?x) (!ride ?t ?x ?y)
    (pay-driver , (+ 1.50 ?d)))
  ((at ?x) (bus-route ?bus ?x ?y))
  `((!wait-for ?bus ?x)
    (pay-driver 1.00)
    (!ride ?bus ?x ?y)))
```

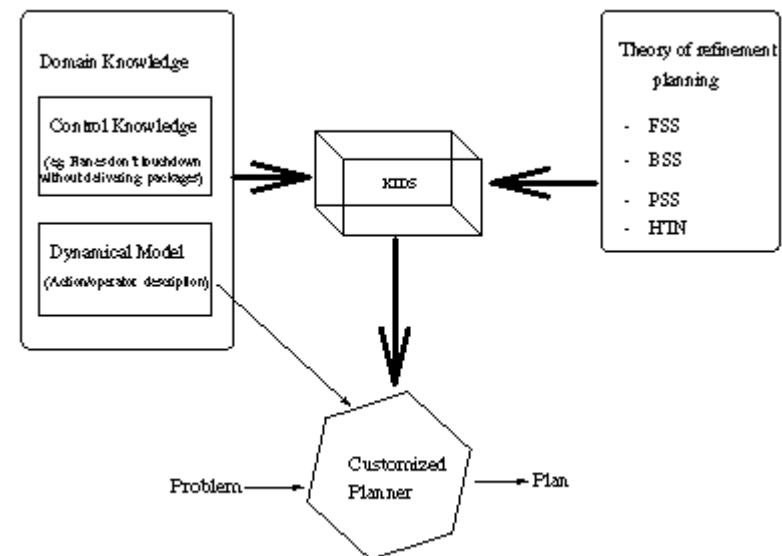
Travel by bus only if going by taxi doesn't work out

***Blurs the domain-specific/domain-independent divide***

**How often does one have this level of knowledge about a domain?**

# Folding the Control Knowledge into the planner: CLAY approach

- ✧ Control knowledge similar to TLPlan's
- ✧ Knowledge is folded using KIDS semi-automated software synthesis tool into a generic refinement planning template
  - Use of program optimizations such as
    - » Finite differencing
    - » Context-dependent & independent simplification
- ✧ Empirical results demonstrate that folding can be better than interpreting rules



Caveat: Current automated software synthesis tools have a very steep learning curve

# Conundrums of user-assisted customization

- ✧ **Which planners are easier to control?**
  - **Conjunctive planners are better if you have search control knowledge**
    - » **Forward State Space (according to TLPlan)**
    - » **Plan-space planners (according to HTN approaches)**
  - **Disjunctive planners are better if your knowledge can be posed as additional constraints on the valid plans**
    - » **Which SAT encoding?**
      - **HTN knowledge is easier to add on top of causal encodings**
- ✧ **Which approach provides the best language for expressing domain knowledge for the lay user?**
  - *(Mine--no, Mine!)*
- ✧ **What type of domain knowledge is easier to validate?**
- ✧ **When does it become “cheating”/ “wishful-thinking”**
  - **Foolish not to be able to use available knowledge**
  - **Wishful to expect deep procedural knowledge...**

# Automated Customization of Planners

- ✧ **Domain pre-processing**
  - Invariant detection; Relevance detection;  
Choice elimination, Type analysis
    - » STAN/TIM, DISCOPLAN etc.
    - » RIFO; ONLP
- ✧ **Abstraction**
  - » ALPINE; ABSTRIPS etc.
- ✧ **Learning Search Control rules**
  - » UCPOP+EBL,
  - » PRODIGY+EBL, (Graphplan+EBL)
- ✧ **Case-based planning (plan reuse)**
  - » DerSNLP, Prodigy/Analogy

*Most of the work has been done in the context of Conjunctive Refinement Planners*

# Symmetry & Invariant Detection

- ✧ **Generate potential invariants and test them**
  - **DISCOPLAN [Gerevini et. al.]**
    - » **Allows detection of higher-order mutexes**
  - **Rintanen's planner**
    - » **Uses model-verification techniques**
  - **STAN/TIM**
    - » **Type analysis of the domain is used to generate invariants**
  - **ONLP (Peot & Smith)**
    - » **Use operator graph analysis to eliminate non-viable choices**

# Abstraction

## ✧ Idea

- Abstract some details of the problem or actions.
- Solve the abstracted version.
- Extend the solution to the detailed version

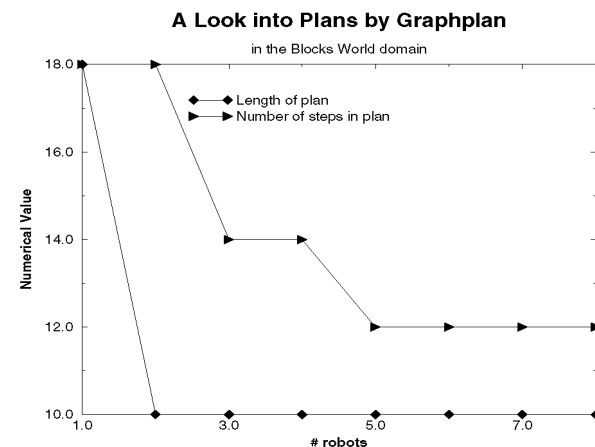
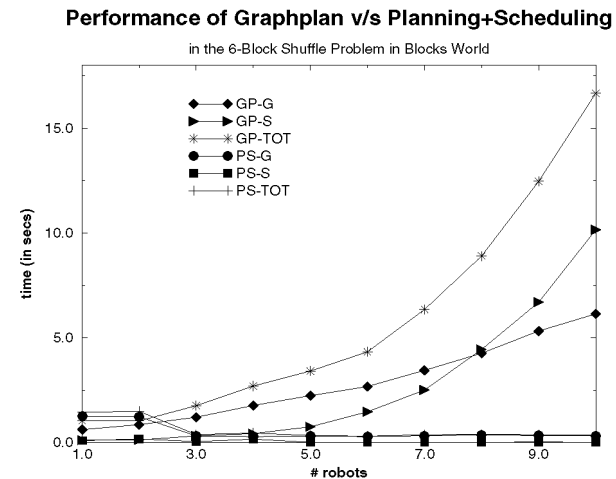
## ✧ Precondition Abstraction

- Work on satisfying *important* preconditions first
  - » Importance judged by:
    - Length of plans for subgoals [ABSTRIPS, PABLO]
    - Inter-goal relations [ALPINE]
    - Distribution-based [HighPoint]
- Strong abstractions (with downward refinement property) are rare
- Effectiveness is planner-dependent
  - » Clashes with other heuristics such as “*most constrained first*”

# Example: Abstracting Resources

- ◇ Most planners thrash by addressing planning and scheduling considerations together
  - Eg. Blocks world, with multiple robot hands
- ◇ Idea: Abstract resources away during planning
  - Plan assuming infinite resources
  - Do a post-planning resource allocation phase
  - Re-plan if needed

(with Biplav Srivastava)



# Learning Search Control Rules with EBL

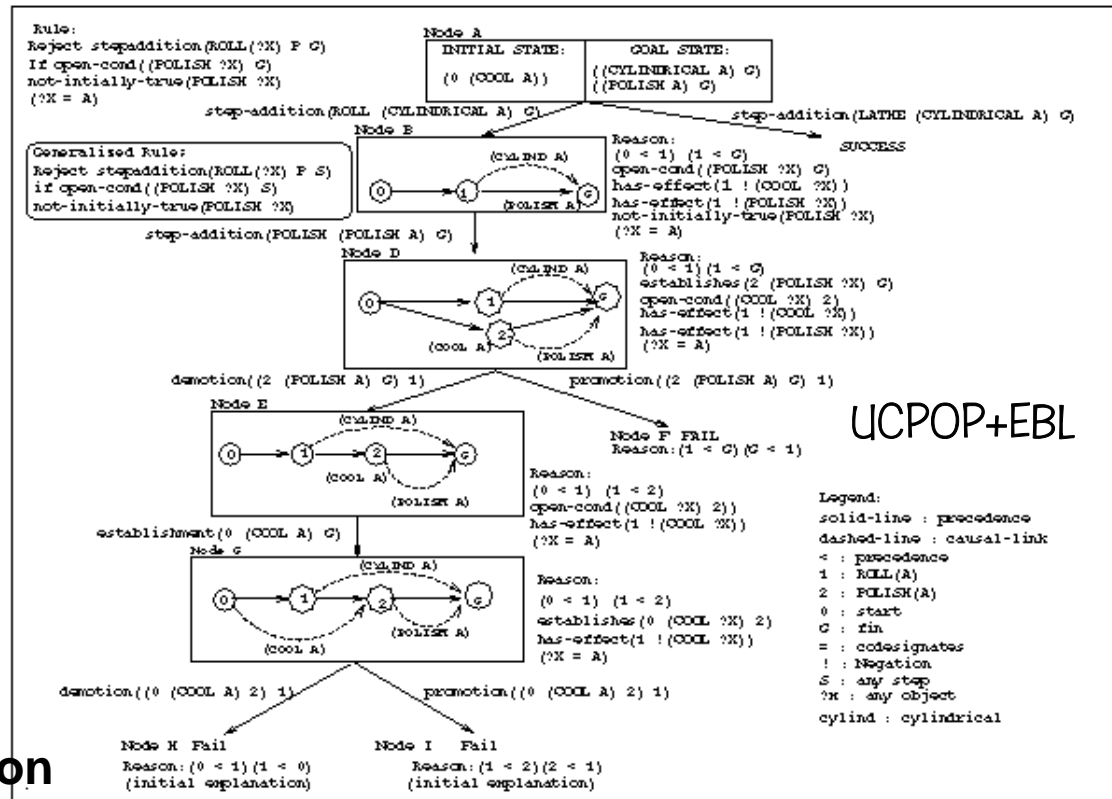
Explain leaf level failures

Regress the explanations to compute interior node failure explanations

Use failure explanations to set up control rules

Problems:

- Most branches end in depth-limits
  - >No analytical explanation
  - >Use preference rules?
- THE Utility problem
  - >Learn general rules
  - >Keep usage statistics & prune useless rules



If Polished(x)@S &  
 ~Initially-True(Polished(x))  
 Then  
**REJECT**  
 Stepadd(Roll(x),Cylindrical(x)@s)

(Kambhampati, Katukam, Qu, 95)



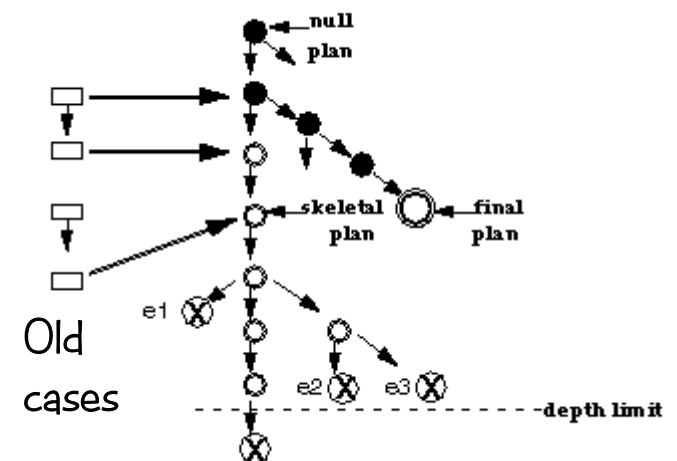
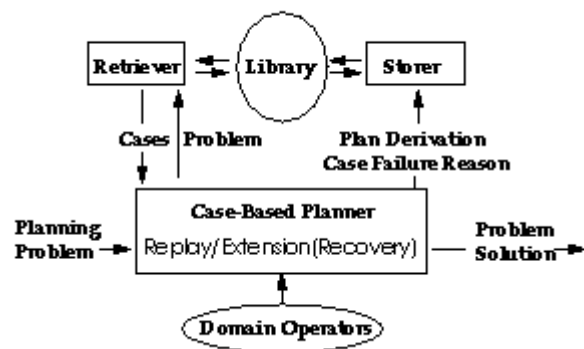
# Case-based Planning

## Macrops, Reuse, Replay

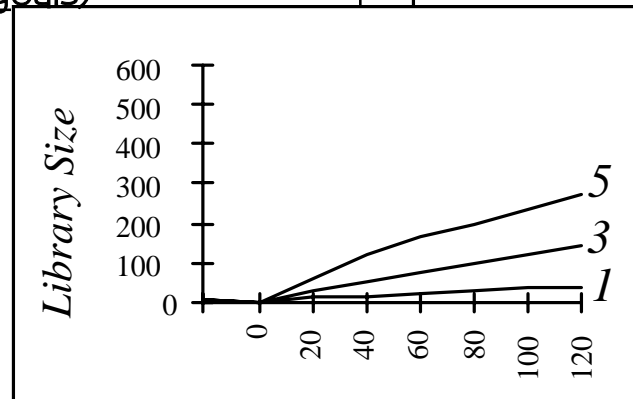
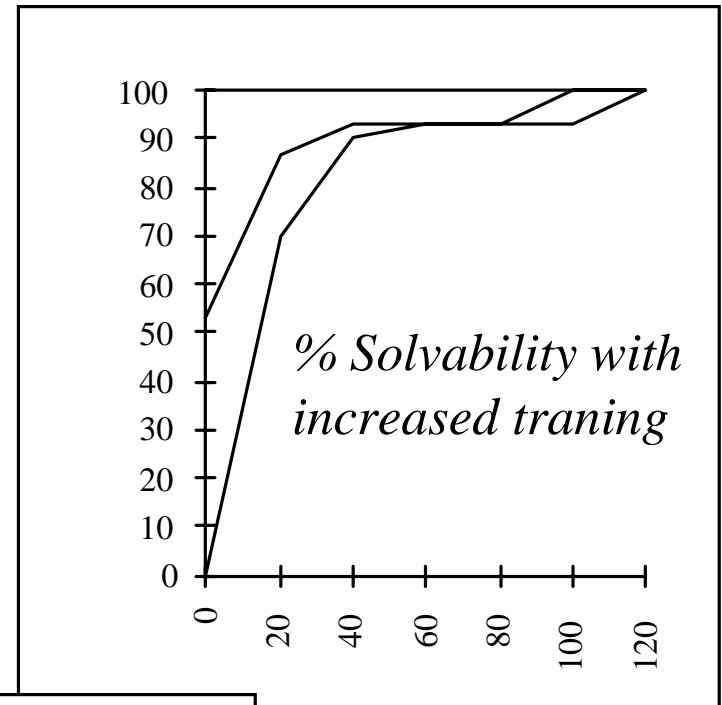
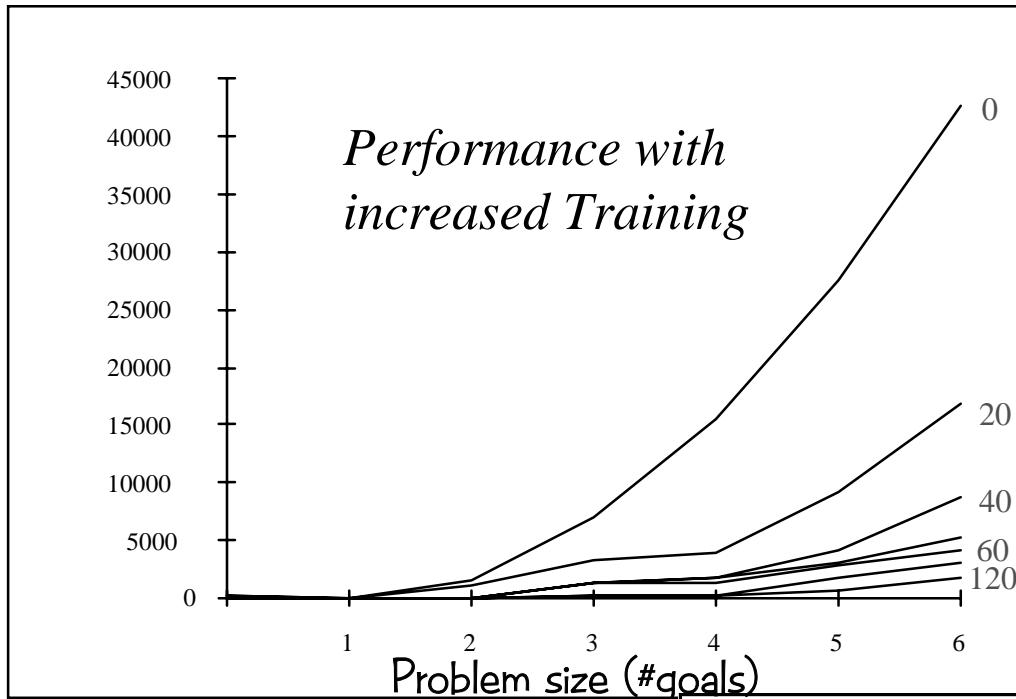
- ✧ **Structures being reused**
  - Opaque vs. Modifiable
  - Solution vs. Solving process (derivation)
- ✧ **Acquisition of structures to be reused**
  - Human given vs. Automatically acquired
- ✧ **Mechanics of reuse**
  - Phased vs. simultaneous
- ✧ **Costs**
  - Storage & Retrieval costs; Solution quality

# Case-study: DerSNLP

- ◇ **Modifiable derivational traces are reused**
- ◇ **Traces are automatically acquired during problem solving**
  - Analyze the interactions among the parts of a plan, and store plans for *non-interacting* subgoals separately
    - » Reduces retrieval cost
  - Use of EBL failure analysis to detect interactions
- ◇ **All relevant trace fragments are retrieved and replayed before the control is given to from-scratch planner**
  - Extension failures are traced to individual replayed traces, and their storage indices are modified appropriately
    - » Improves retrieval accuracy



# DerSNLP: Results



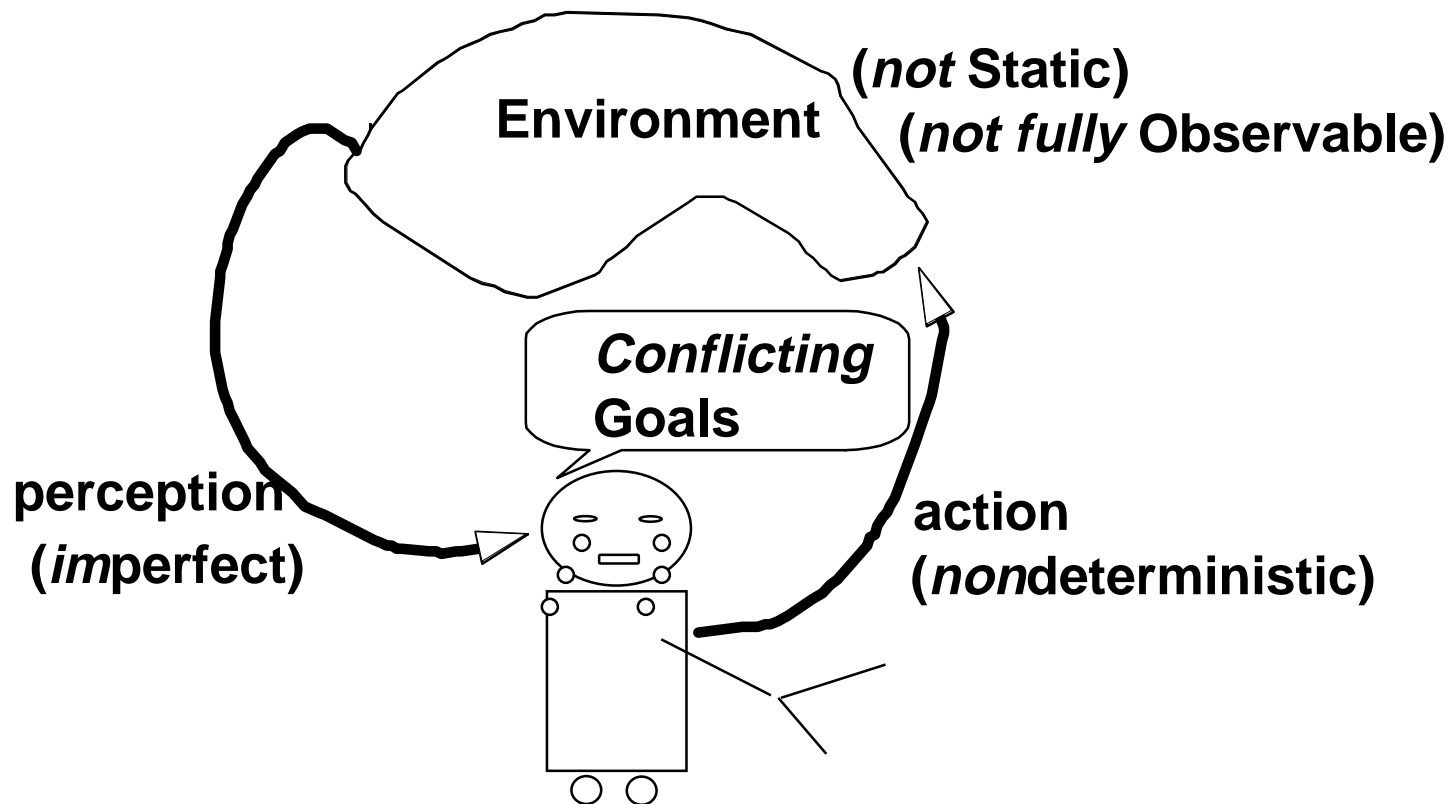
(JAIR, 97)

# Reuse in Disjunctive Planning

- ✧ **Harder to make a disjunctive planner commit to extending a specific plan first**
- ✧ **Options:**
  - **Support opaque macros along with primitive actions**
    - » **Increases the size of k-step disjunctive plan**
    - » **But a solution may be found at smaller k**
  - **Modify the problem/domain specification so the old plan's constraints will be respected in any solution (Bailotti et. al.)**
  - **MAX-SAT formulations of reuse problem**
    - » **Constrain the encoding so that certain steps may have smaller step-action mapping and ordering choices**
    - » **Causal encodings provide better support**

*[with Amol Mali]*

# Connections to Non-Classical Planning

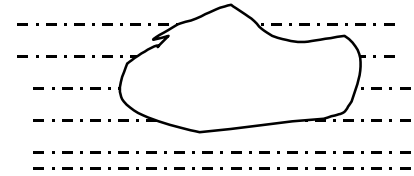


*The most efficient approaches to all these *ills* are still based on classical planning ideas...*

# Metric and Temporal constraints

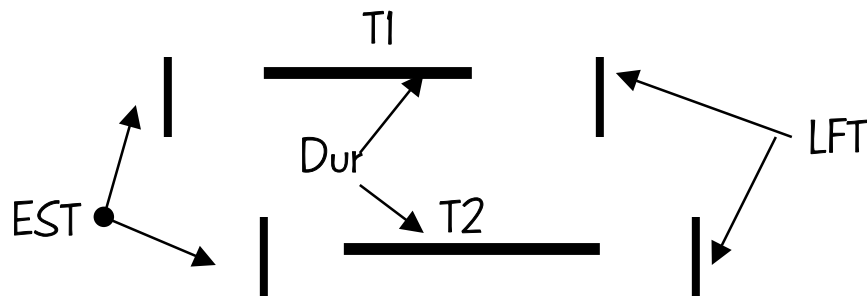
- ✧ **Problem: Most real-world problems involve actions with durations, goals with deadlines, continuous resources**
  - While still being observable, deterministic and static
- ✧ **APPROACHES:**
  - Handling numeric/continuous quantities
    - » LPSAT [Wolfman & Weld; 99] integrates a SAT solver with an LP solver
      - ZENO [Penberthy & Weld; AAI-94] extends UCPOP
    - » ILP encodings [Vossen & Nau; 99; Kautz & Walser; 99]
  - Handling actions with durations
    - » TGP [Smith & Weld; 99] supports actions with durations in Graphplan
  - Integrate planning & scheduling; postpone durations, resources etc. to scheduling phase
    - » [Srivastava & Kambhampati; 99]

# Scheduling as CSP



## Jobshop scheduling

- Set of jobs
  - » Each job consists of tasks in some (partial) order
- Temporal constraints on jobs
  - » EST, LFT, Duration
- Contention constraints
  - » Each task can be done on a subset of machines



## CSP Models

- Tasks as variables
  - » Time points as values
  - » EST, LFT, Machine contention as constraints
- Inter-task precedences as variables

## CSP Techniques

- Customized consistency enforcement techniques
  - » ARC-B consistency
- Customized variable/value ordering heuristics
  - » Contention-based
  - » Slack-based
- MaxCSP; B&B searches

# Incomplete Information

- ✧ **PROBLEM:** Values of some state variables are unknown; There are actions capable of sensing (some) of them.
  - If  $k$  boolean state variables are unknown, then we are in one of  $2^k$  initial states
  - Two naïve approaches
    - » **PLAN/SENSE/EXECUTE** : Solve each of the  $2^k$  problems separately; At the execution time sense the appropriate variables, and execute the appropriate plan
    - » **SENSE/PLAN/EXECUTE**: First sense the values of the variables. Solve the problem corresponding to the sensed values
  - Problems with naïve approaches
    - » Solving the  $2^k$  problems separately is wasteful
      - Shared structure (Tree structured plans)
    - » Not all variables may be observable (or worth observing)
      - Conformant planning
        - (Find non-sensing plans that work in all worlds)
      - Irrelevant variables (Goal directed planning)



# Incomplete Information: Some Implemented Approaches

## ✧ Conjunctive planners

- CNLP [Peot & Smith; 92] CASSANDRA [Pryor & Collins, 96] add sensing actions to UCPOP; support tree-shaped plans
- SADL/PUCCINI [Golden & Weld; 96-98] integrates planning and sensing in the context of a UCPOP-like planner

## ✧ Disjunctive planners

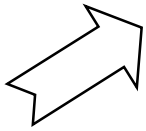
- CGP [Smith & Weld, 98] supports conformant planning on Graphplan
- SGP [Weld et. al., 98] supports conditional planning on Graphplan
  - » One plan-graph per possible world/ Interactions among plangraphs captured through induced mutexes
- [Rintanen, 99] converts conditional planning to QBF encodings

# Dynamic Environments

✧ **PROBLEM:** The world doesn't sit still. Blind execution of a "correct" plan may not reach goals

✧ **APPROACHES:**

– **PLAN/MONITOR/REPLAN:** Monitor the execution; when the observed state differs from the expected one, REPLAN



» Replanning is like reuse except there is added incentive for minimal modification

● Easy to support with conjunctive plan-space planners

– PRIAR [Kambhampati; 92]; DerSNLP [Ihrig & Kambhampati, 97]

● Possible to support with disjunctive causal encodings

– [Mali & Kambhampati]

– **MONITOR/REACT/LEARN:**

» Policy construction (Universal plans)...

– **MODEL OTHER AGENTS CAUSING CHANGE:**

» Collaborative/Distributed planning

# Stochastic Actions

- ✧ **PROBLEM:** Action effects are stochastic
  - Actions transform *state-distributions* to state-distributions
  - Maximize “probability” of goal satisfaction
  - Plan assessment itself is hard
- ✧ **APPROACHES:**
  - Conjunctive planners
    - » BURIDAN [Hanks et. al., 95] uses UCPOP techniques to put candidate plans together and assesses them
      - *Multiple /redundant supports*
  - Disjunctive planners
    - » Pgraphplan [Blum & Langford, 98] modifies Graphplan to support some forms of stochastic planning
      - Forward search; value propagation
    - » Maxplan [Majercik & Littman, 98] uses EMAJSAT encodings to solve stochastic planning problems
      - Chance variables & Choice variables. Equivalence classes of models that have the same values of choice variables. Find the equivalence class with maximum probability mass.

# Complex & Conflicting Goals

## ✧ Problems & Solutions:

- **Goals that have temporal extent (stay alive)**
  - » UCPOP, TLPlan, TGP [Smith& Weld, 99]
- **Goals that have mutual conflicts (Sky-dive & Stay Alive)**
- **Goals that take cost of achievement into account**
- **Goals that admit degrees of satisfaction (Get rich)**
  - » **Branch & Bound approaches; MAXSAT approaches**
    - **Pyrrhus [Williamson & Hanks; 92]**

### Decision Theoretic Approaches:

Model goals in terms of factored reward functions  
for Markov Decision Processes

--Can utilize tricks and insights from classical planning  
[Boutilier, Hanks, Dean; JAIR 99]

# Summary

- ✧ **Refinement planning provides a unifying view**
  - **Conjunctive Refinement Planners**
    - » **Effective heuristics**
  - **Disjunctive Refinement Planners**
    - » **Refinement**
    - » **Solution Extraction**
      - **Direct vs. compilation to CSP/SAT**
  - **Tradeoffs, Acceleration techniques**
- ✧ **Customization of planners**
  - **User-assisted**
  - **Automated**
- ✧ **Related approaches to non-classical planning**

# Status

- ✧ **Exciting times...**
  - Many approaches with superior scale-up capabilities
    - » Broadened views of planning
  - Many influences (CSP; OR; MDP; SCM)
- ✧ **Ripe for serious applications**
  - VICAR [JPL]; DeepSpace monitoring [NASA/AMES]
  - Plant monitoring [Ayslett et. al.]
  - Manufacturing Process Planning [Nau et. al.; Kambhampati et. al]
  - Supply chain management/ Logistics
    - » Industrial “Planning” does not have to the optimal scheduling of an inoptimal action selection!

# Resources

## ✧ Mailing Lists

- Planning list digest
  - » <http://rakaposhi.eas.asu.edu/planning-list-digest>
- U.K. P & S List
  - » <http://www.salford.ac.uk/planning/home.html>

## ✧ Special Conferences

- Intl. Conf. on AI Planning & Scheduling
  - » <http://www.isi.edu/aips> (April 2000, Breckenrdige, CO)
- European Conference on Planning
  - » <http://www.informatik.uni-ulm.de/ki/ecp-99.html>
- Also, AAI, IJCAI, ECAI, Spring/Fall Symposia

## ✧ Courses

- ASU Planning Seminar Online Notes (1999, 1997, 1995, 1993)
  - » <http://rakaposhi.eas.asu.edu/planning-class.html>